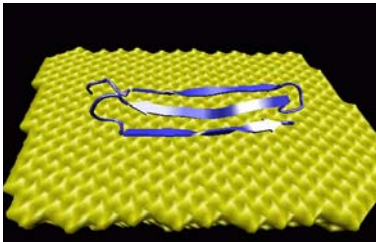
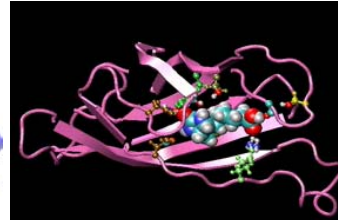
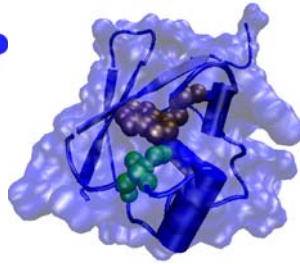
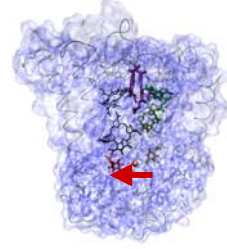
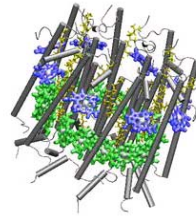
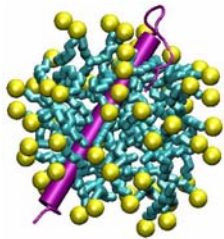


# What can be learnt from MD

Gold binding protein

Micelle Light harvesting complex Reaction Center

Restriction enzyme Ubiquitin avidin-biotin



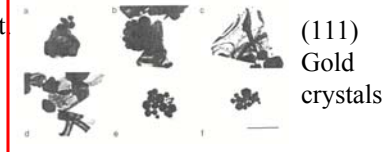
## Gold Binding Protein: 1. Structure Prediction

Protein-mineral interaction is of interest from biological and materials science perspectives:

Teeth, abalone shells, or nanomaterials

Proteins have been genetically engineered which bind to Au and alter crystal morphology (GBPs). Binding mechanism unknown; structure prediction and molecular dynamics simulations may provide insight

Best binders: multiple repeats of 14 amino acids; lead to Au crystals with dominant (111) surfaces; rich in polar amino acids serine and threonine.



GBP-1: Anti-parallel $\beta$ -sheet (high confidence).	
H-K	M   HGKTQATSGTIQSM   HGKTQATSGTIQSM   HGKTQATSGTIQSM   HGK
Sim	Similar sequences have $\beta$ -sheet structure.

3 repeats

Holley-Karplus (HK) and alignment (Sim) results. In the sequences, blue signifies beta sheet and black signifies random coil.

# Gold Binding Protein - 2. Simulation

Molecular dynamics carried out using the program NAMD2.

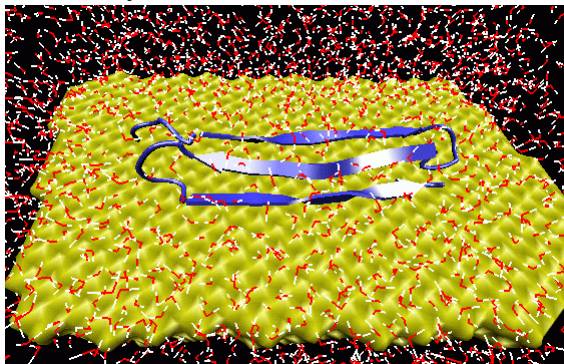
Au surfaces created with known FCC structure and 4.07Å lattice spacing;

Total system size: ~13,000 atoms.

GBP sequence mapped to β-sheet and manually positioned on Au surface;

Force field: CHARMM22, TIP3P water, periodic boundary conditions, full electrostatics (PME)

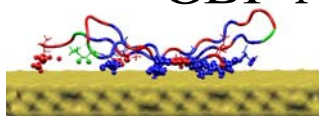
Constant pressure and temperature. Au held fixed.



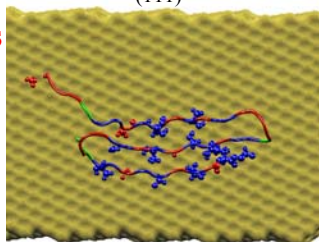
$$U_{surf} = 2\pi \sum_{l=0}^{\infty} n_l \epsilon \sigma^2 \left[ \frac{2}{5} \left( \frac{\sigma}{z + d_l} \right)^{10} - \left( \frac{\sigma}{z + d_l} \right)^4 \right]$$

## GBP-Au Contacts

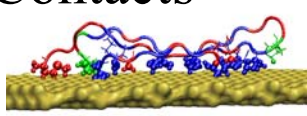
Useful insights for new design!



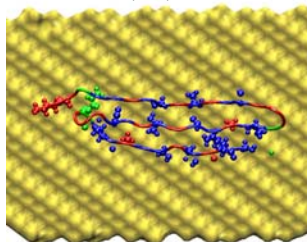
(111)



less interstitial water

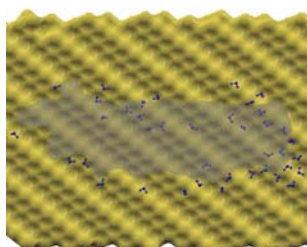


(211)



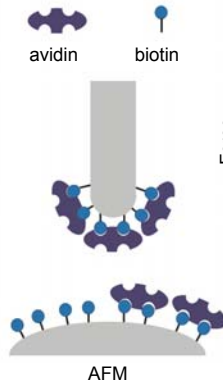
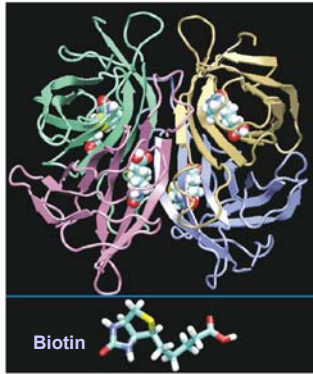
surface contacts: polar amino acids Thr, Ser

repeats exhibit additive interaction

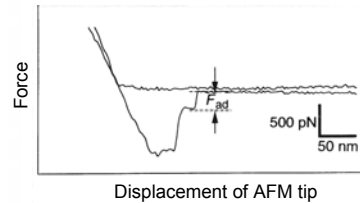


more interstitial water

# Atomic Force Microscopy Experiments of Ligand Unbinding



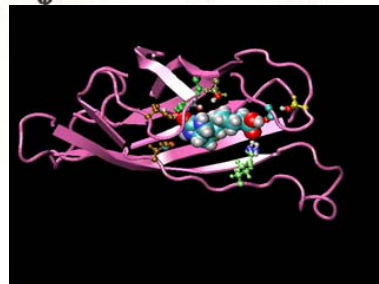
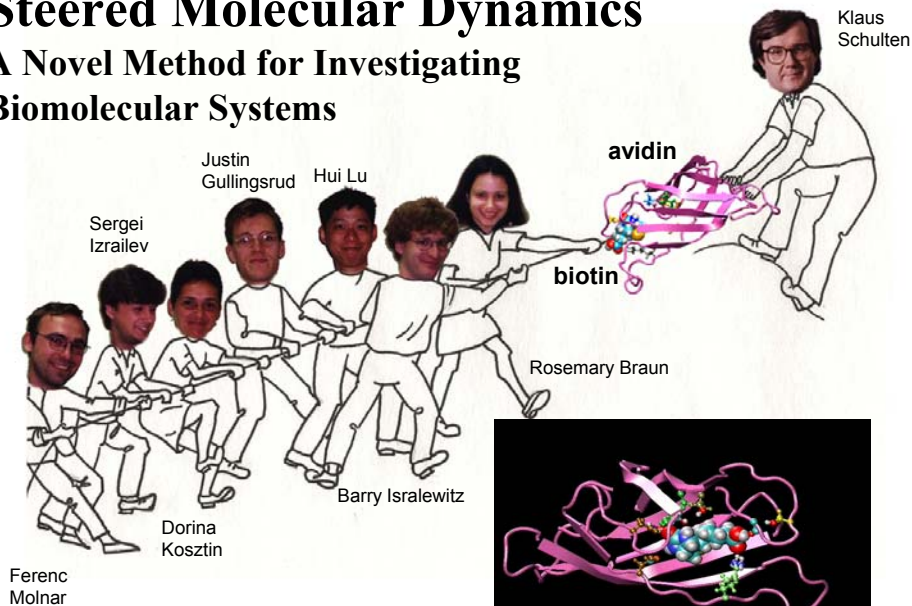
Florin et al., Science 264:415 (1994)



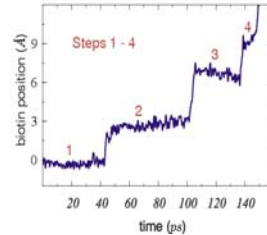
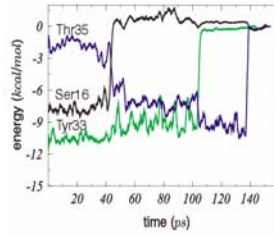
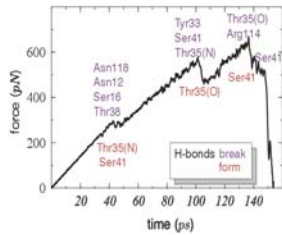
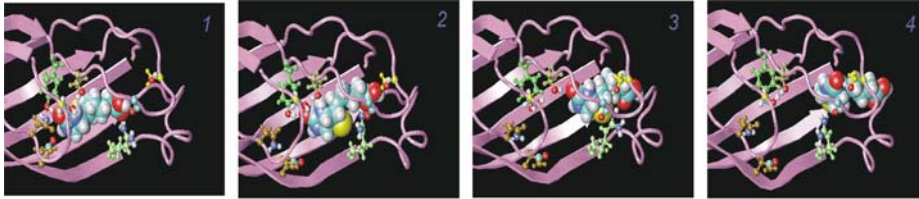
*NIH Resource for Macromolecular Modeling and Bioinformatics  
Theoretical Biophysics Group, Beckman Institute, UIUC*

# Steered Molecular Dynamics

## A Novel Method for Investigating Biomolecular Systems



## Atomic Force Microscopy and Steered Molecular Dynamics Complement Each Other !



Israilev *et al.*, *Biophys. J.*, **72**, 1568-1581 (1997)

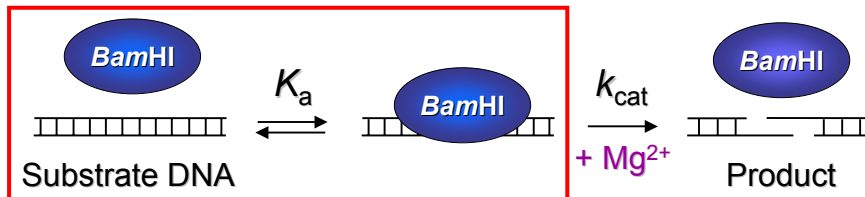
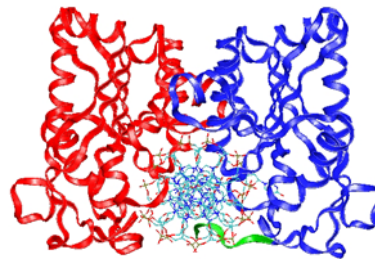
<http://www.ks.uiuc.edu>

NIH Resource for Macromolecular Modeling and Bioinformatics  
Theoretical Biophysics Group, Beckman Institute, UIUC

## Type II Restriction Endonuclease - *Bam*HI

213 a.a./monomer  
Binds the recognition sequence:  
5'-G<sup>1</sup>GATCC-3'

Newman, M. *et al.* (1995)  
*Science* **269**, 656-663

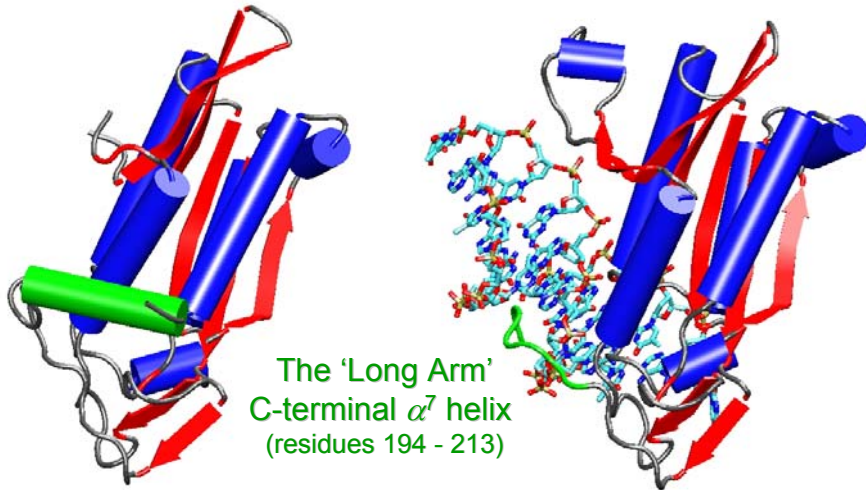


Cognate DNA :  $K_d \sim 600 \text{ pM}$



Substrate Free

Specific Complex



Newman, M. *et al.* (1994) *Structure* **2**, 439-452  
Newman, M. *et al.* (1995) *Science* **269**, 656-663

Cray T3E



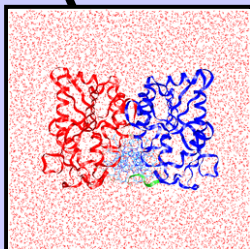
Th. Lynch,  
S. Sligar,  
D. Kosztin

High pressure gel electrophoresis

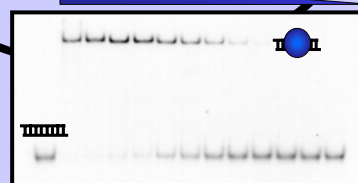


Theory

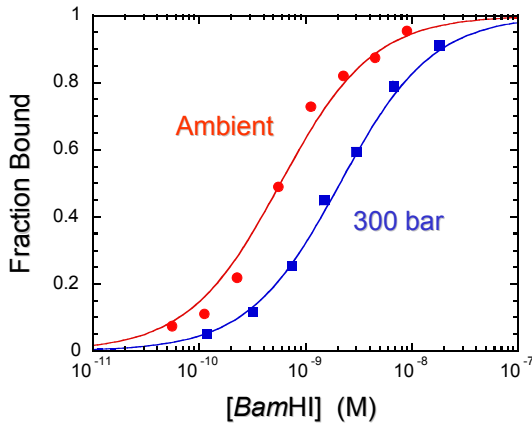
Experiment



[Protein]



## Hydrostatic Pressure Effect on $K_d$

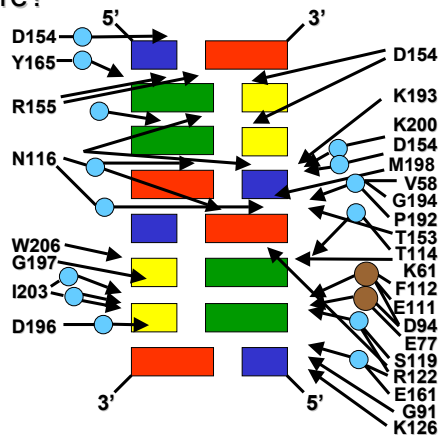
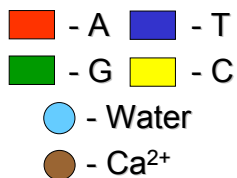


$K_d$ (nM)	P (bar)
$0.7 \pm 0.1$	1
$1.5 \pm 0.1$	150
$2.5 \pm 0.3$	300
$4.6 \pm 0.4$	500

## Pressure Effects on Specific Interactions

How do we identify the individual structural elements that are affected by pressure?

X-ray analysis  
Direct and Water Mediated  
Contacts



Interaction energies between *BamHI* and DNA

# Molecular Dynamic Simulations

Particle Mesh Ewald    Periodic Boundary Conditions

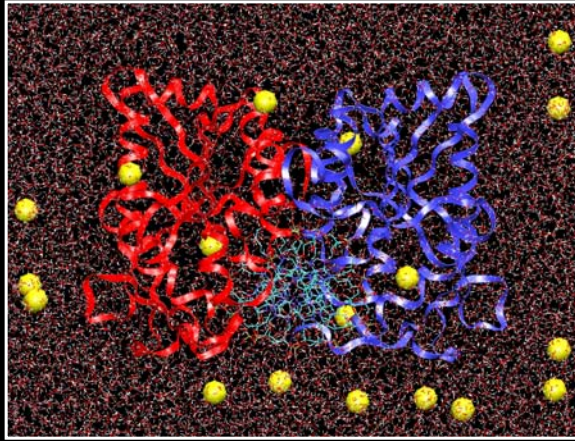
NpT ensemble

Pressure control: Nose-Hoover

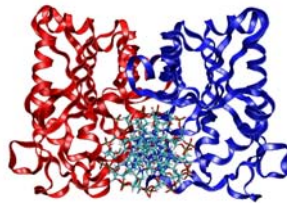
> 65,000 atoms

32 counterions -  $\text{Na}^+$

1 ns trajectories

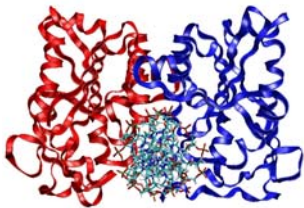


Simulation  
snapshots



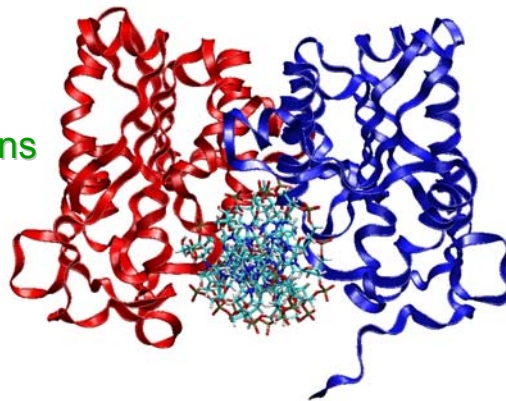
t = 0

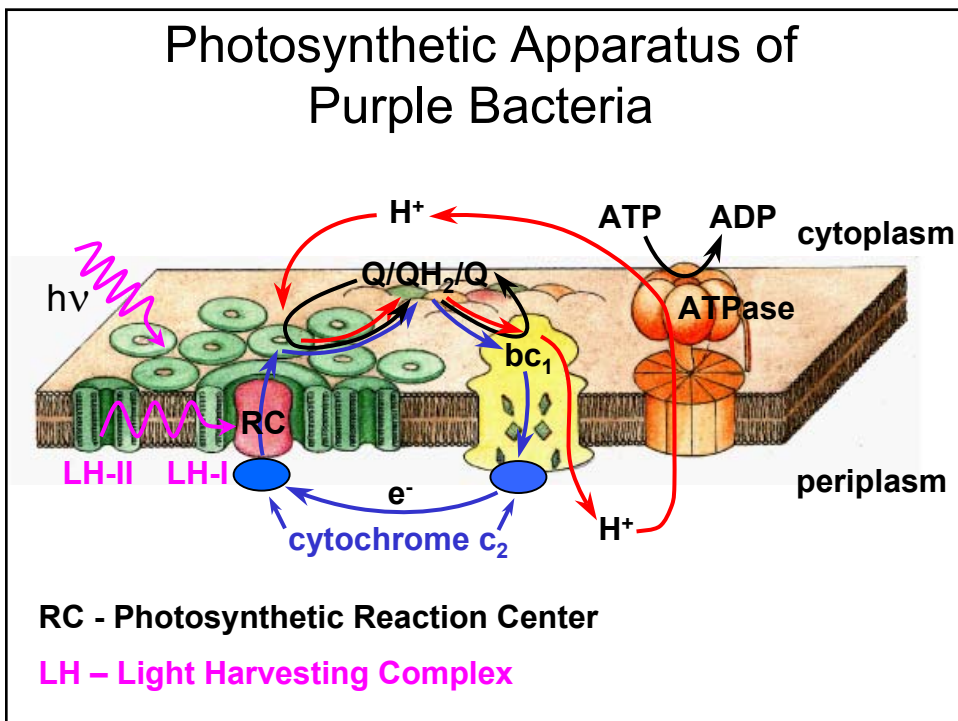
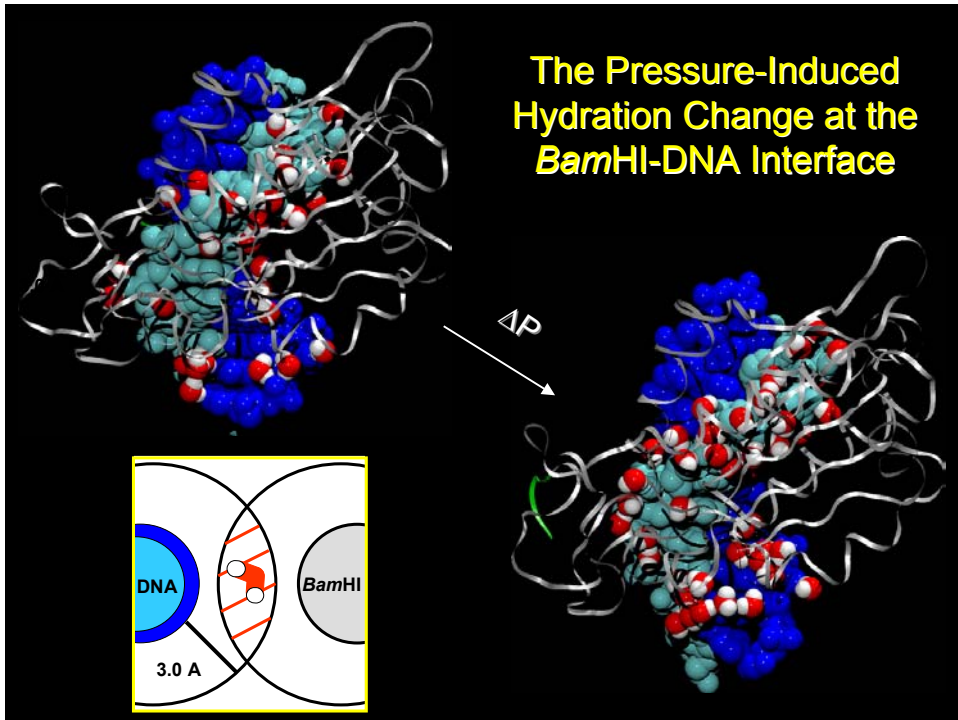
Ambient pressure



t = 1 ns

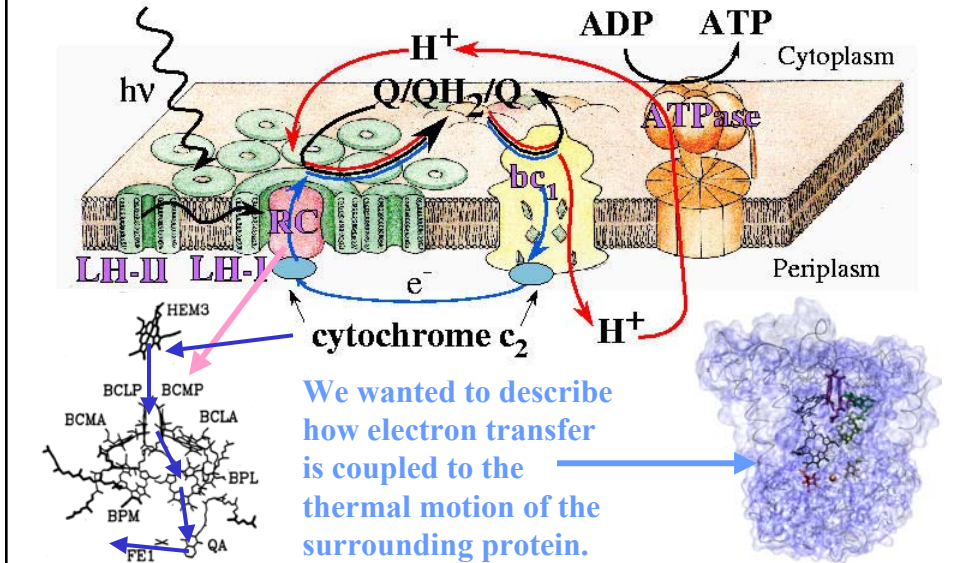
P ~ 400 bar







## Role of Thermal Disorder on Electron Transfer in the Photosynthetic Reaction Center



## Electron Transfer Process Coupled to the Protein Matrix

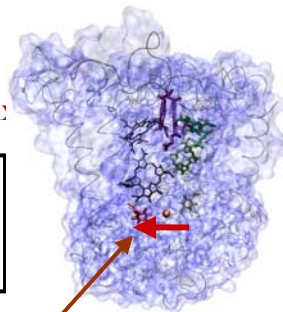
We assumed that the electron transfer  $Q_A^- Q_B \rightarrow Q_A Q_B^-$  is coupled to an **ensemble of oscillators representing the protein matrix**:

$$\text{Hamiltonian} \quad \hat{H}_{q_0}^{(s)} = \begin{pmatrix} \hat{H}_r^{(s)} & v \\ v & \hat{H}_p^{(s)} + E \end{pmatrix}$$

Protein matrix is a bath of oscillators linearly coupled to the electron transfer according to

$$\hat{H}_r = \sum_j \left( \frac{\hat{p}_j^2}{2M_j} + \frac{1}{2} M_j \omega_j^2 q_j^2 \right)$$

$$\hat{H}_p = \sum_j \left( \frac{\hat{p}_j^2}{2M_j} + \frac{1}{2} M_j \omega_j^2 \left( q_j - \frac{c_j}{M_j \omega_j^2} \right)^2 \right)$$



Dong Xu and Klaus Schulten. *Chemical Physics*, 182: 91--117, 1994.

Klaus Schulten. In D. Bicout and M. J. Field, editors, *Proc. Ecole de Physique des Les Houches*, pp 85--118, Les Editions de Physique, Springer, Paris, 1995.

Klaus Schulten. *Science*, 290:61--62, 2000.

## Electron Transfer Process Coupled to the Protein Matrix

Rate for an ensemble of oscillators (spin boson model, Legett et al)

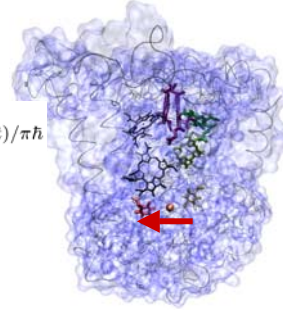
$$k_{qb}(R \rightarrow P) = \frac{v^2}{\hbar^2} \int_{-\infty}^{+\infty} dt e^{itE/\hbar} e^{iQ_1(t)/\pi\hbar} e^{-Q_2(t)/\pi\hbar}$$

Relaxation rate

$$k_{\text{rel}} = \frac{2v^2}{\hbar^2} \int_0^{+\infty} dt \cos(tE/\hbar) \cos(Q_1(t)/\pi\hbar) e^{-Q_2(t)/\pi\hbar}$$

$$Q_1(t) = \frac{\pi}{2} \sum_j \frac{c_j^2}{\hbar\omega_j^3} \sin\omega_j t$$

$$Q_2(t) = \frac{\pi}{2} \sum_j \frac{c_j^2}{\hbar\omega_j^3} \coth\frac{\hbar\omega_j}{2kT} [1 - \cos(\omega_j t)]$$



But we didn't know all the coupling constants  $c_j$ ? All we needed to know was  $J$

$$J(\omega) = \frac{\pi}{2} \sum_j \frac{c_j^2}{\omega_j} \delta(\omega - \omega_j) \quad Q_1(t) = \int_0^\infty d\omega \omega^{-2} J(\omega) \sin\omega t$$

$$Q_2(t) = \frac{\pi}{2} \int_0^\infty d\omega \omega^{-2} J(\omega) \coth\frac{\hbar\omega}{2kT} (1 - \cos\omega t)$$

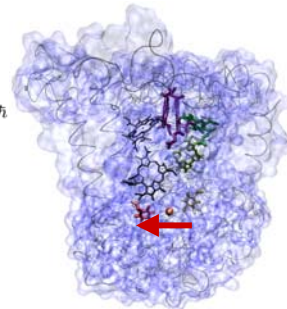
## Electron Transfer Process Coupled to the Protein Matrix

Relaxation rate

$$k_{\text{rel}} = \frac{2v^2}{\hbar^2} \int_0^{+\infty} dt \cos(tE/\hbar) \cos(Q_1(t)/\pi\hbar) e^{-Q_2(t)/\pi\hbar}$$

$$Q_1(t) = \int_0^\infty d\omega \omega^{-2} J(\omega) \sin\omega t$$

$$Q_2(t) = \frac{\pi}{2} \int_0^\infty d\omega \omega^{-2} J(\omega) \coth\frac{\hbar\omega}{2kT} (1 - \cos\omega t)$$



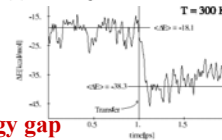
$$\frac{J(\omega)}{\omega} = \frac{\sigma^2}{k_B T} \int_0^\infty dt C(t) \cos\omega t \quad \text{1994}$$

$$C_{\epsilon\epsilon}(t) = \frac{\langle (\epsilon(t) - \langle \epsilon \rangle) (\langle \epsilon(0) - \langle \epsilon \rangle) \rangle}{\langle \epsilon(0) - \langle \epsilon \rangle \rangle^2}$$

**energy gap correlation function**

$\sigma$  rms deviation of energy gap

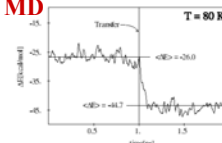
$$\epsilon(t) = \hat{H}_p - \hat{H}_r + E$$



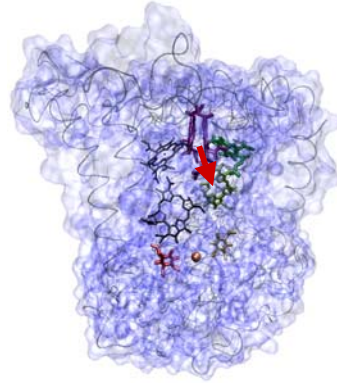
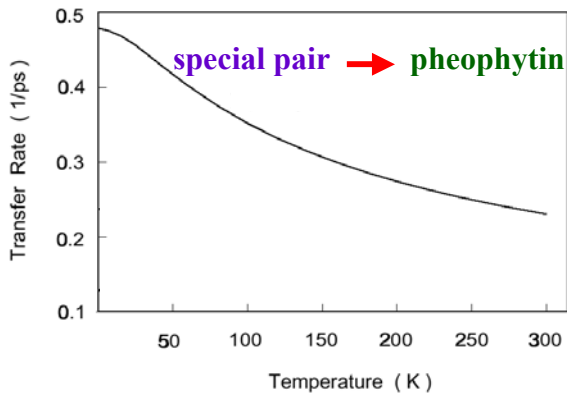
energy gap

from MD

1989

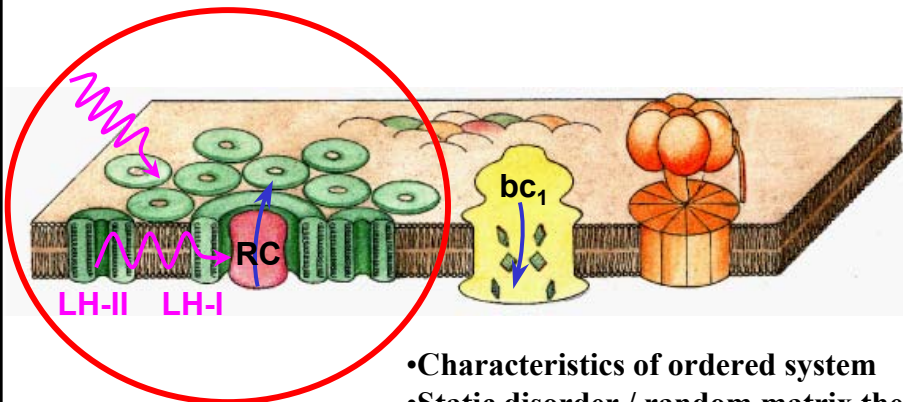


## Temperature Dependence of Electron Transfer Rate



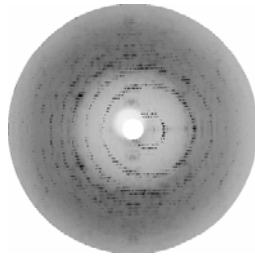
Dong Xu

## How does the Light Harvesting System Function with Thermal Disorder?

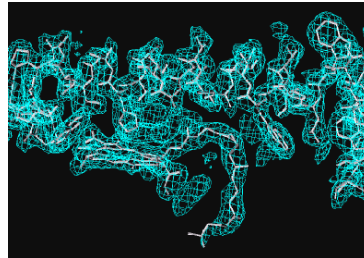


- Characteristics of ordered system
- Static disorder / random matrix theory
- Dynamics disorder / linear response th.
- Dynamic disorder / polaron model
- Role of carotenoids

# Structure of LH-II of *Rs. molischianum* Obtained Through a Computationally Derived Search Model



molecular  
replacement

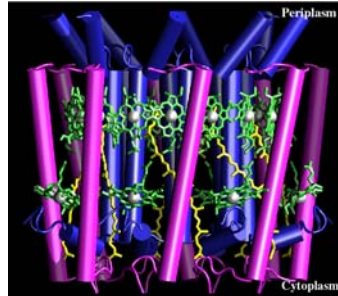


## Summary of Crystallographic Data

- space group P4212
- resolution range 8-2.4 Å
- unique reflection 30309
- completeness 87.2
- R-factor (%) 21.1
- free R-factor (%) 23.2

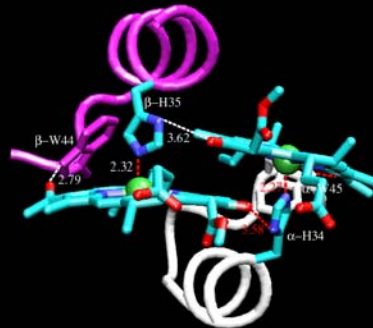
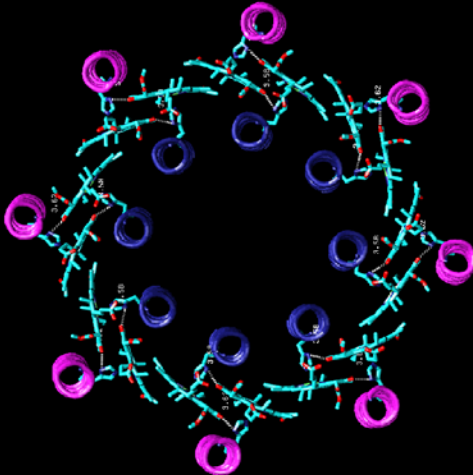
Koepke et al., Structure, 4, 581 (1996)

Xiche Hu



## B850 BChls of LH-II of *Rs. molischianum*

**New aggregation pattern of chlorophylls, first discovered by R. Cogdell et al in LH-II of *Rps. acidophila***

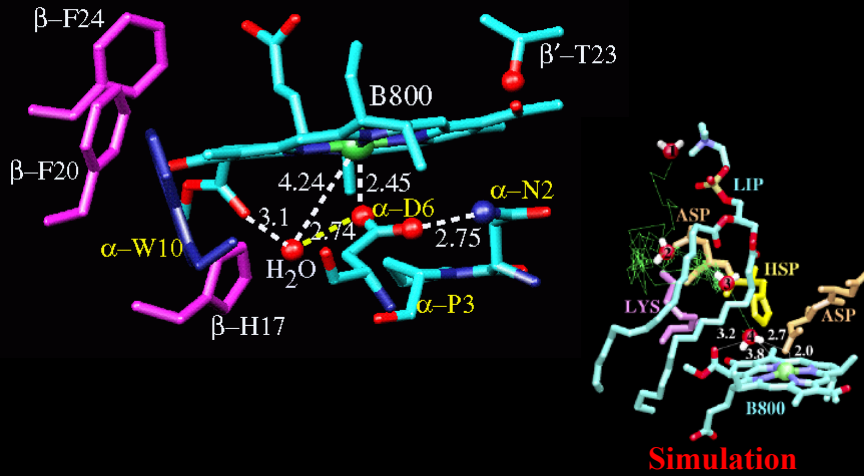


Spectrum tuned through local and excitonic interactions as well as disorder



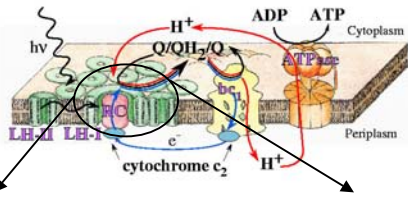
# B800 BChl-a Binding Site

**New ligation pattern of chlorophyll's Mg atom!**

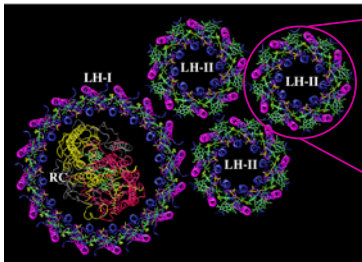


## The light harvesting system displays a hierarchy of integral, functional units

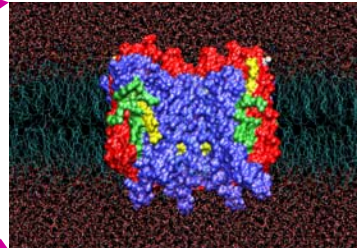
Photosynthetic membrane generates ATP using light energy



Hu and Schulten, *Biophys J.*, **75**, 683-694 (1998)  
 Ritz *et al.*, *J. Lumin.*, **76-77**, 310-321 (1998)  
 Hu *et al.*, *PNAS*, **95**, 5935-5941 (1998)  
 Koepke *et al.*, *Structure*, **4**, 581-597 (1996)  
 Hu *et al.*, *J. Phys. Chem.*, **B 101**, 3854-3871 (1997)  
 Cory *et al.*, *J. Phys. Chem.*, **B 102**, 7640-7650 (1998)  
 Damjanovic *et al.*, *Phys. Rev. E*, **59**, 3293-3311 (1999)



Light harvesting unit funnels excitation energy to photosynthetic reaction center

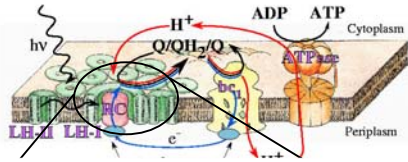


Light harvesting complex II absorbs light and converts it into electronic excitations of BChls

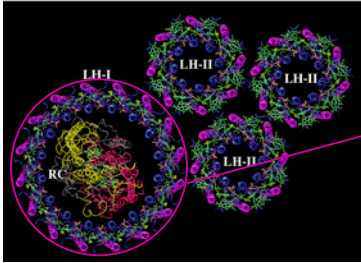
Molecular modeling of integral, functional units with more than  $10^6$  atoms necessary

## The light harvesting system displays a hierarchy of integral, functional units

Photosynthetic membrane generates ATP using light energy



- Hu and Schulten, *Biophys. J.*, **75**, 683-694 (1998)
- Ritz *et al.*, *J. Lumin.*, **76-77**, 310-321 (1998)
- Hu *et al.*, *PNAS*, **95**, 5935-5941 (1998)
- Koepke *et al.*, *Structure*, **4**, 581-597 (1996)
- Hu *et al.*, *J. Phys. Chem.*, **B 101**, 3854-3871 (1997)
- Cory *et al.*, *J. Phys. Chem.*, **B 102**, 7640-7650 (1998)
- Damjanovic *et al.*, *Phys. Rev. E*, **59**, 3293-3311 (1999)

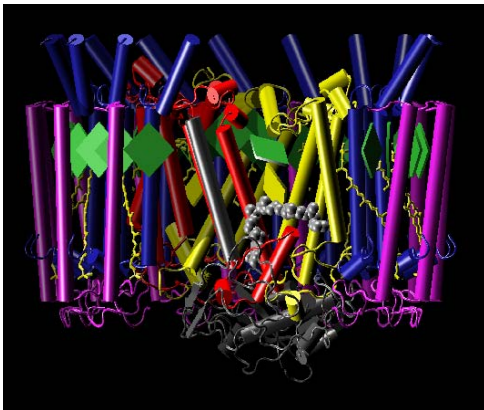


We need to know also the structure of the LH-I ring! We use again modeling, replacing subunit of LH-II by that of LH-I

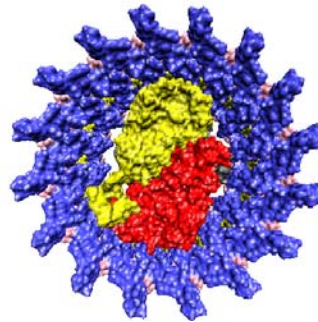
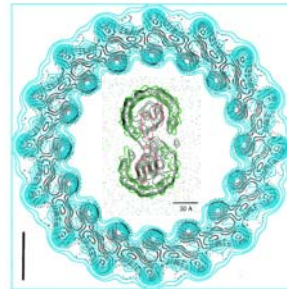
Molecular modeling of integral, functional units with more than  $10^6$  atoms necessary

## LH-I – RC Complex of *Rb. Sphaeroides*

Model agrees well with EM map

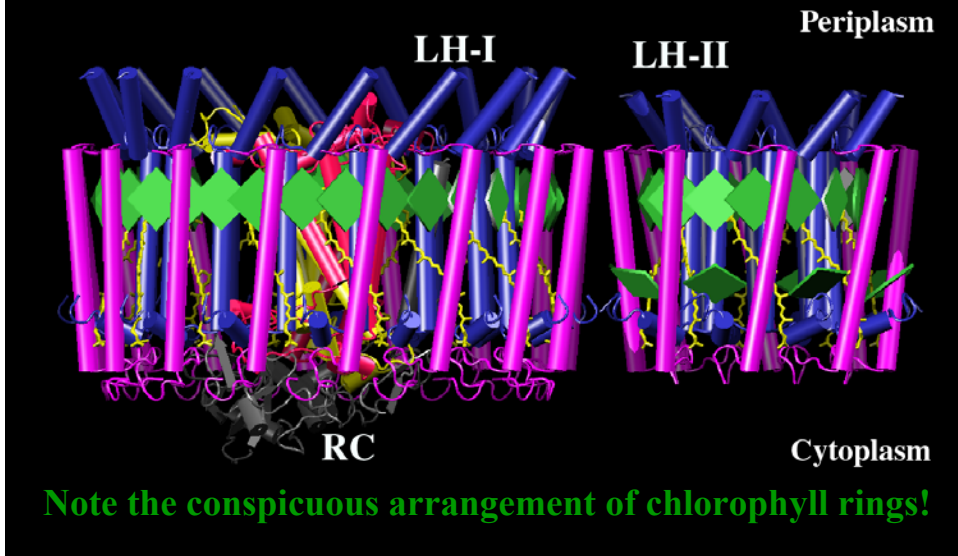


Xiche Hu

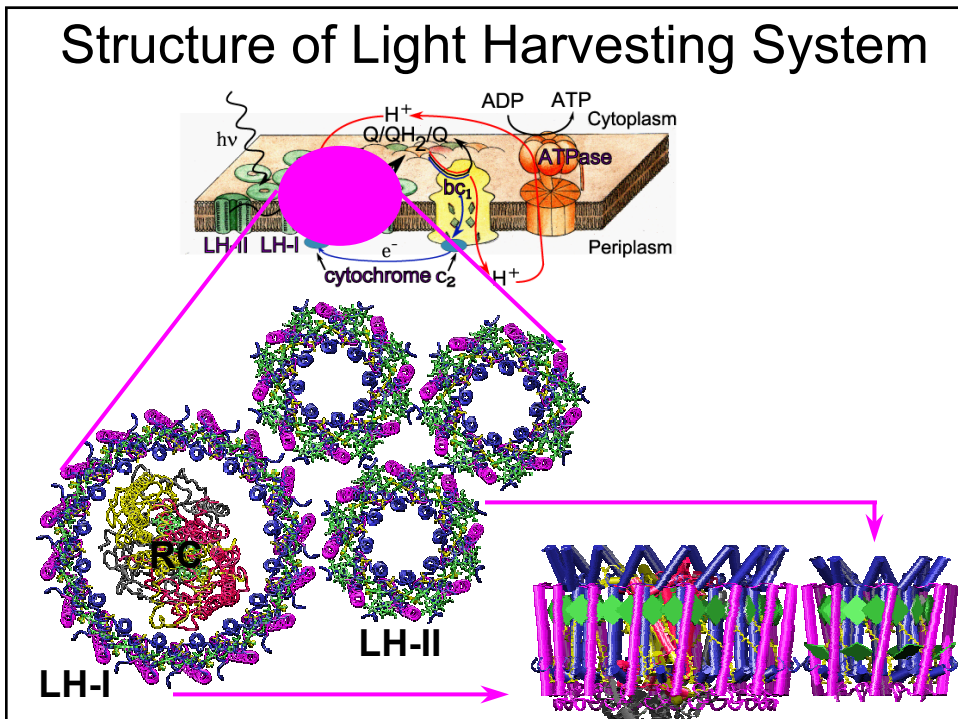


View from top

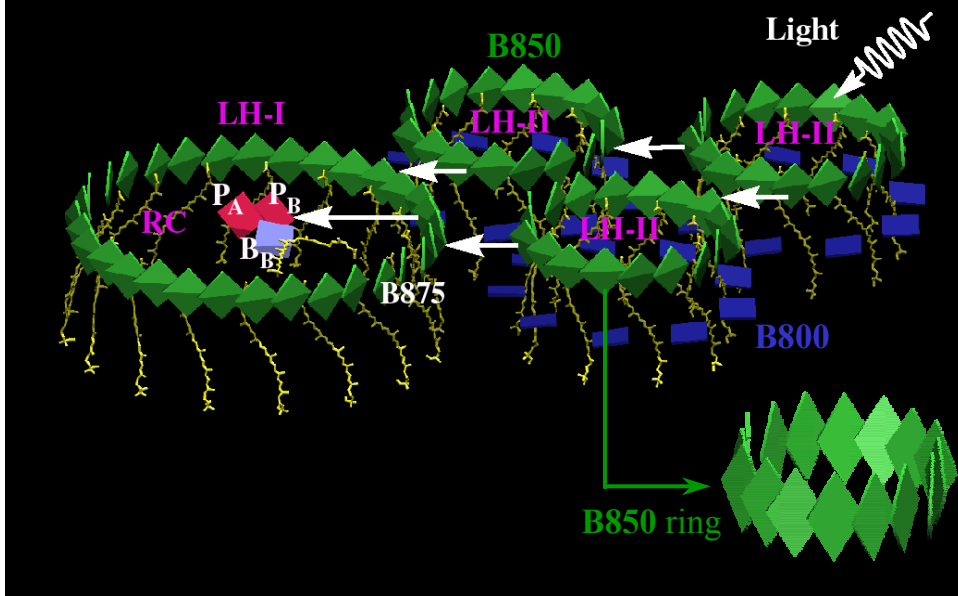
# Pigment Organization in the Bacterial Photosynthetic Membrane



# Structure of Light Harvesting System



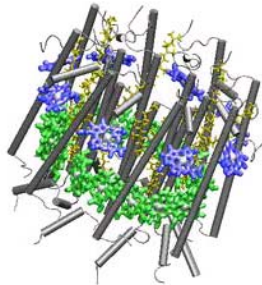
# Hierarchical aggregate of *chromophores*



## The Effect of Dynamic Disorder

Molecular Dynamics (MD) Simulation

Gaussian 98, HF/CIS, STO-3G basis

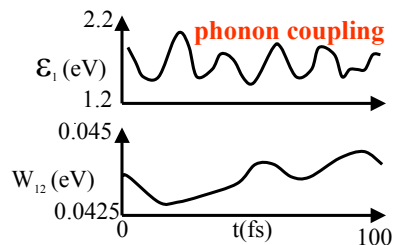


LH2 in membrane: 85,000 atoms;  
equilibrated for 2ns with NAMD2;  
NpT ensemble; periodic boundary  
condition; full electrostatics (PME)

Followed by 0.8ps simulation,  
trajectory output every 2fs with  
quantum chemistry calc. of exc.  
energy, interpolated to "sample"  
every 0.5 fs

$$\hat{H}(t)^{exc} = \begin{pmatrix} \epsilon_1(t) & & \\ & \epsilon_2(t) & \\ & & \ddots \\ & & & \epsilon_{16}(t) \end{pmatrix} W_{ij}(t)$$

$$W_{jk} = C \left( \frac{\vec{d}_j \cdot \vec{d}_k}{r_{jk}^3} - \frac{3(\vec{r}_{jk} \cdot \vec{d}_j)(\vec{r}_{jk} \cdot \vec{d}_k)}{r_{jk}^5} \right)$$



Ana Damjanovic, Ioan Kosztin, Ulrich Kleinekathoefer, and Klaus Schulten, Phys. Rev. E (submitted)

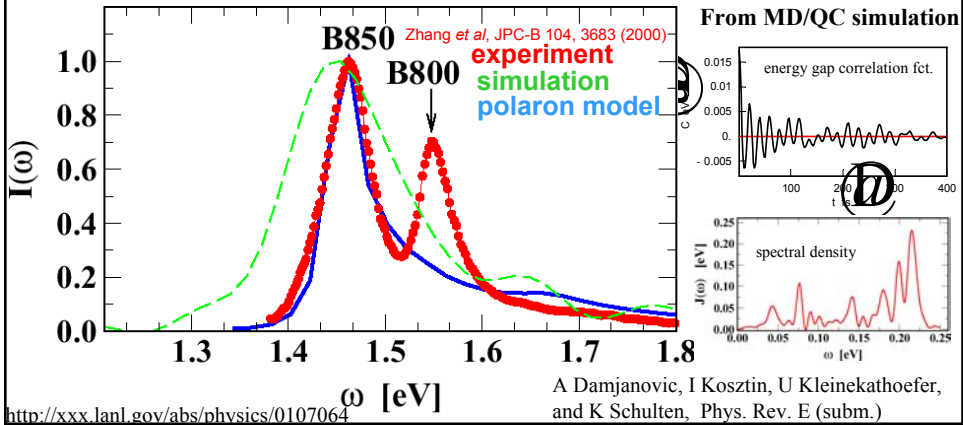


# Absorption Spectrum – B850 Excitons

$$I(\omega) \propto \sum_k |d_k|^2 \int_0^\infty dt \exp[-\Phi'_k(t)] \cos[(\omega - \epsilon_k)t + \Phi''_k(t)]$$

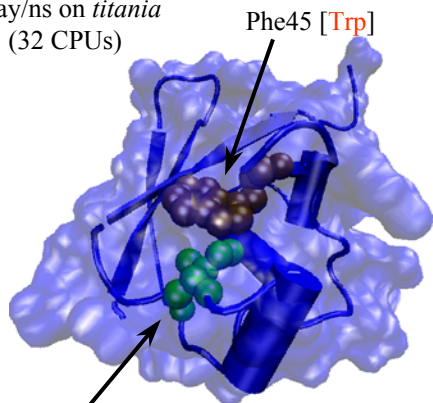
$$\Phi_k(t) = \int_0^t d\tau (t - \tau) \mathcal{D}(\tau) F_k(\tau)$$

↗ phonon contribution  
↘ exciton contribution



# Folding of Ubiquitin

10,000 atoms  
1 day/ns on *titania*  
(32 CPUs)



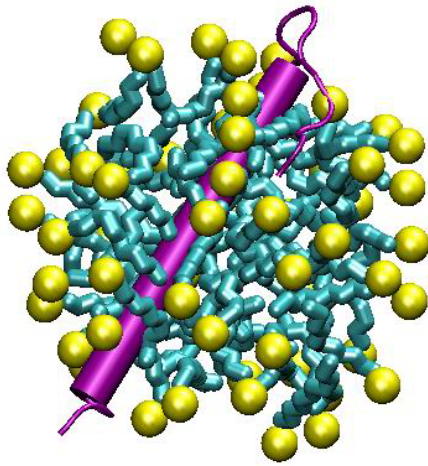
Mutations:  
Val61 – MD simulations  
Ala61 – experiment and MD simulations

## Edgar Larios

- Collaborator:  
**M. Gruebele**, UIUC
- Goals:
  - Experimental and MD studies of the folding of *ubiquitin*
  - Ultrafast fluorescence study of **Trp45** in ubiquitin
- Result:
  - Explained the anisotropy of the fluorescence spectra of **Trp** in different mutants of ubiquitin

**Edgar Larios**

# Helix Interaction in Micelle



Micellar sphere of 60 SDS molecules  
30,000 atoms

## Rosemary Braun

- Collaborator:  
**D. Engelman**, Yale Univ.
- Goals:
  - Examine stability of single and two helices in micelle with respect to mutations
- Results:
  - Equilibrated micell
  - Built the helices

Rosemary Braun, Justin Gullingsrud