GPU Computing Case Study: Molecular Modeling Applications

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Outline

- General introduction to GPU computing
- Explore CUDA algorithms for computing electrostatic fields around molecules
  - Detailed look at CUDA implementations of a simple direct Coulomb summation algorithm
  - Multi-GPU direct Coulomb summation
  - Cutoff (range-limited) summation algorithm
- CUDA acceleration of parallel molecular dynamics simulation on GPU clusters with NAMD
- Wrap-up

Evolution of Graphics Hardware Towards Programmability

- As graphics accelerators became more powerful, an increasing fraction of the graphics processing pipeline was implemented in hardware
- For performance reasons, this hardware was highly optimized and task-specific
- Over time, with ongoing increases in circuit density and the need for flexibility in lighting and texturing, graphics pipelines gradually incorporated programmability in specific pipeline stages
- Modern graphics accelerators are now processors in their own right (thus the new term “GPU”), and are composed primarily of large arrays of programmable processing units

Programmable Graphics Hardware

Groundbreaking research systems:

AT&T Pixel Machine (1989):

82 x DSP32 processors

UNC PixelFlow (1992-98):

64 x (PA-8000 +

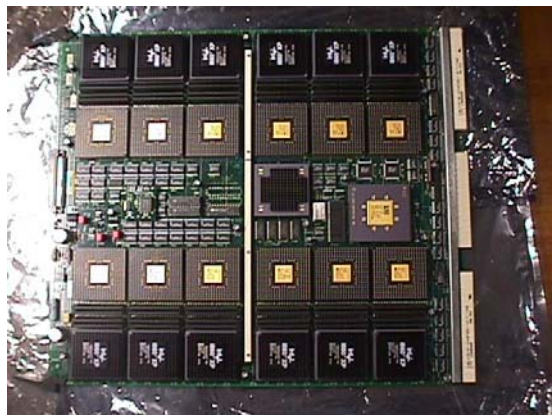
8,192 bit-serial SIMD)

SGI RealityEngine (1990s):

Up to 12 i860-XP processors perform vertex operations (*u*code), fixed-func. fragment hardware

All mainstream GPUs now incorporate programmable processors

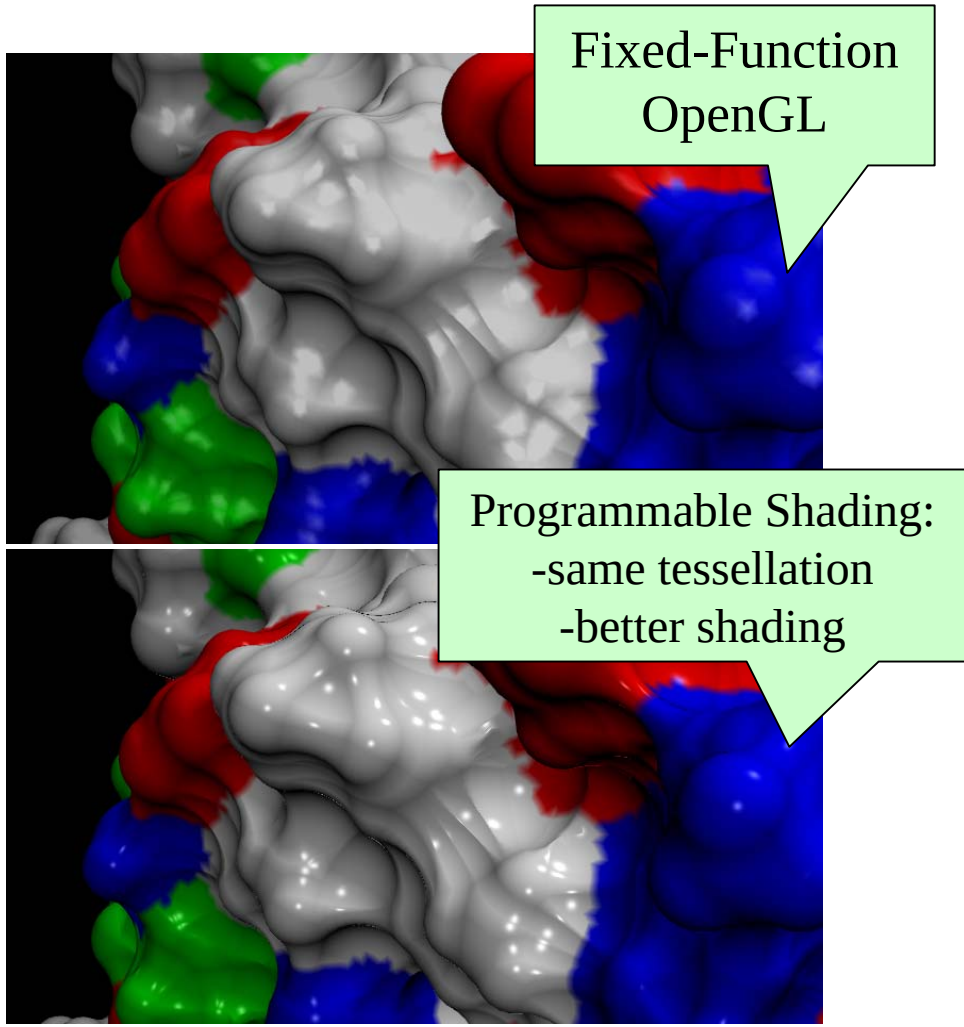
UNC PixelFlow Rack



Reality Engine Vertex Processors

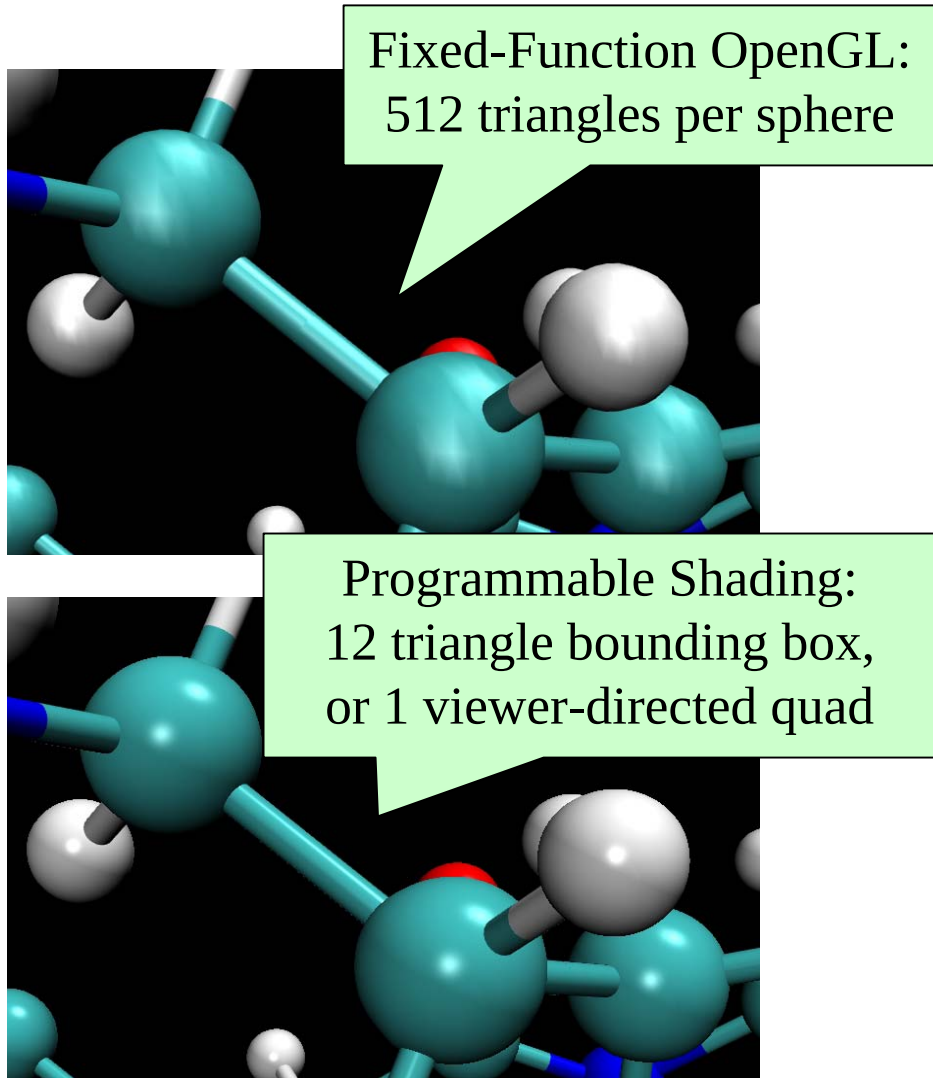
Benefits of Programmable Shading

- Potential for superior image quality with better shading algorithms
- Direct rendering of:
  - Quadric surfaces
  - Volumetric data
- Offload work from host CPU to GPU

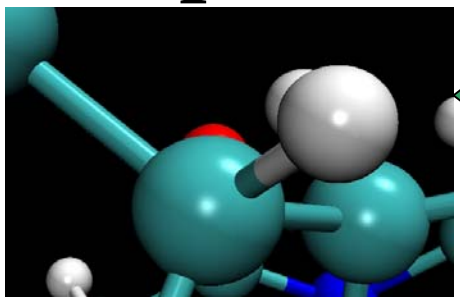


Ray Traced Sphere Rendering with Programmable Shading

- Fixed-function OpenGL requires curved surfaces to be tessellated with triangles, lines, or points
- Fine tessellation required for good results with Gouraud shading; performance suffers
- Static tessellations look bad when viewer zooms in
- Programmable shading solution:
  - Ray trace spheres in fragment shader
  - GPU does all the work
  - Spheres look good at all zoom levels
  - Rendering time is proportional to pixel area covered by sphere
  - Overdraw is a bigger penalty than for triangulated spheres



Sphere Fragment Shader



- Written in OpenGL Shading Language
- High-level C-like language with vector types and operations
- Compiled dynamically by the graphics driver at *runtime*
- Compiled machine code executes on GPU

```
//
// VMD Sphere Fragment Shader (not for normal geometry)
//
void main(void) {
  vec3 raydir = normalize(V);
  vec3 spheredir = spherepos - rayorigin;

  // Perform ray-sphere intersection tests based on the code in Tachyon
  float b = dot(raydir, spheredir);
  float temp = dot(spheredir, spheredir);
  float disc = b*b + sphereradsq - temp;

  // only calculate the nearest intersection, for speed
  if (disc <= 0.0)
    discard; // ray missed sphere entirely, discard fragment

  // calculate closest intersection
  float tnear = b - sqrt(disc);

  if (tnear < 0.0)
    discard;

  // calculate hit point and resulting surface normal
  vec3 pnt = rayorigin + tnear * raydir;
  vec3 N = normalize(pnt - spherepos);

  // Output the ray-sphere intersection point as the fragment depth
  // rather than the depth of the bounding box polygons.
  // The eye coordinate Z value must be transformed to normalized device
  // coordinates before being assigned as the final fragment depth.
  if (vmdprojectionmode == 1) {
    // perspective projection = 0.5 + (hfpn + (f * n / pnt.z)) / diff
    gl_FragDepth = 0.5 + (vmdprojparms[2] + (vmdprojparms[1] * vmdprojparms[(
3];
  } else {
    // orthographic projection = 0.5 + (-hfpn - pnt.z) / diff
    gl_FragDepth = 0.5 + (-vmdprojparms[2] - pnt.z) / vmdprojparms[3];
  }

#ifdef TEXTURE
  // perform texturing operations for volumetric data
  // The only texturing mode that applies to the sphere shader
```

Use of GPUs For Computation

- Widespread support for programmable shading led researchers to begin experimenting with the use of GPUs for general purpose computation, “GPGPU”
- Early GPGPU efforts used existing graphics APIs to express computation in terms of drawing
- As one would expect, expressing general computation problems in terms of triangles and pixels and “drawing the answer” is obfuscating and painful to debug to say the least…
- Soon researchers began creating dedicated GPU programming tools, starting with Brook and Sh, and ultimately leading to a variety of commercial tools such as CUDA

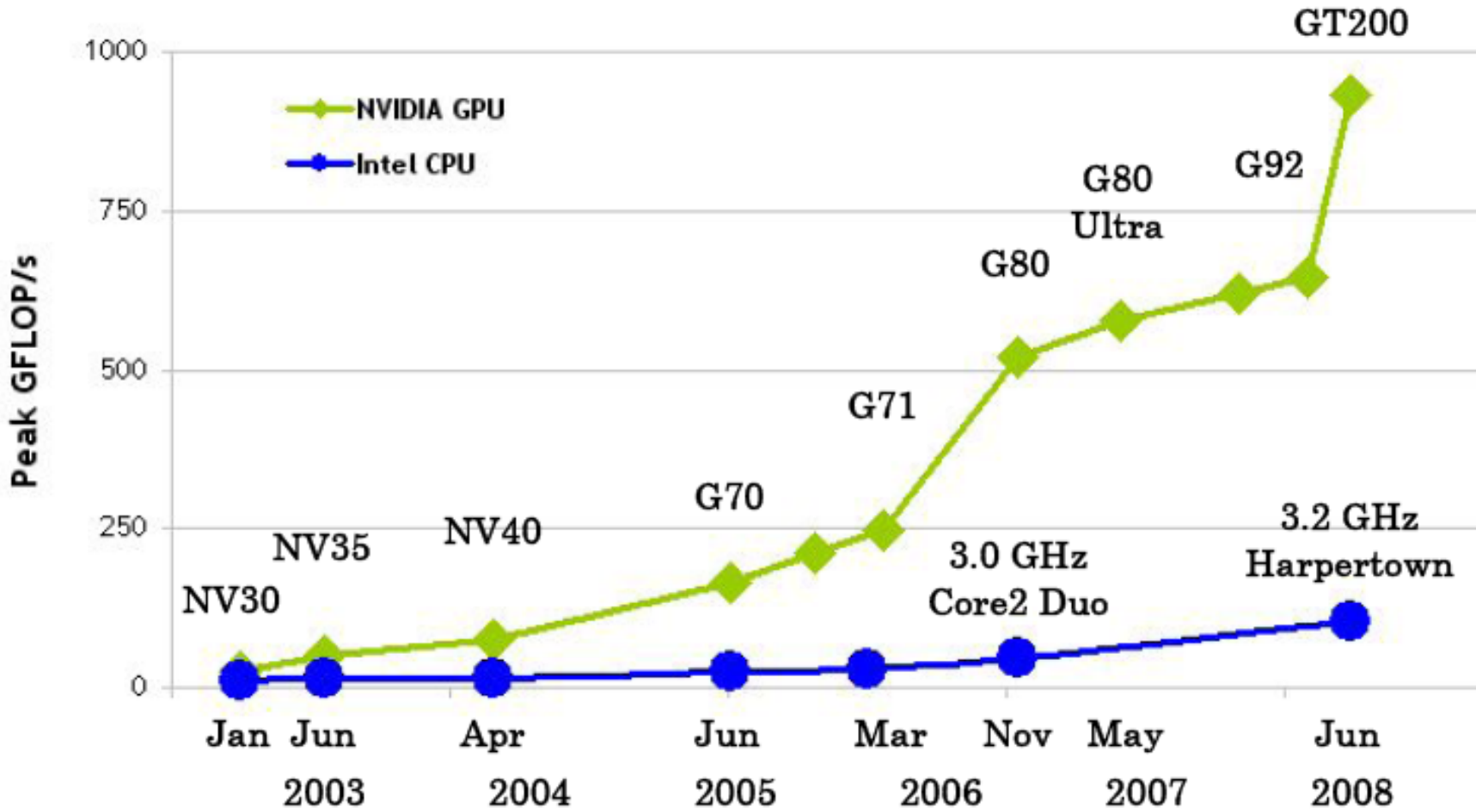
GPU Computing

- Commodity devices, omnipresent in modern computers
- Massively parallel hardware, hundreds of processing units, throughput oriented design
- Support all standard integer and floating point types
- Programming tools allow software to be written in dialects of familiar C/C++ and integrated into legacy software
- GPU algorithms are often multicore-friendly due to attention paid to data locality and work decomposition, and can be successfully executed on multi-core CPUs as well, using special runtime systems (e.g. MCUDA)

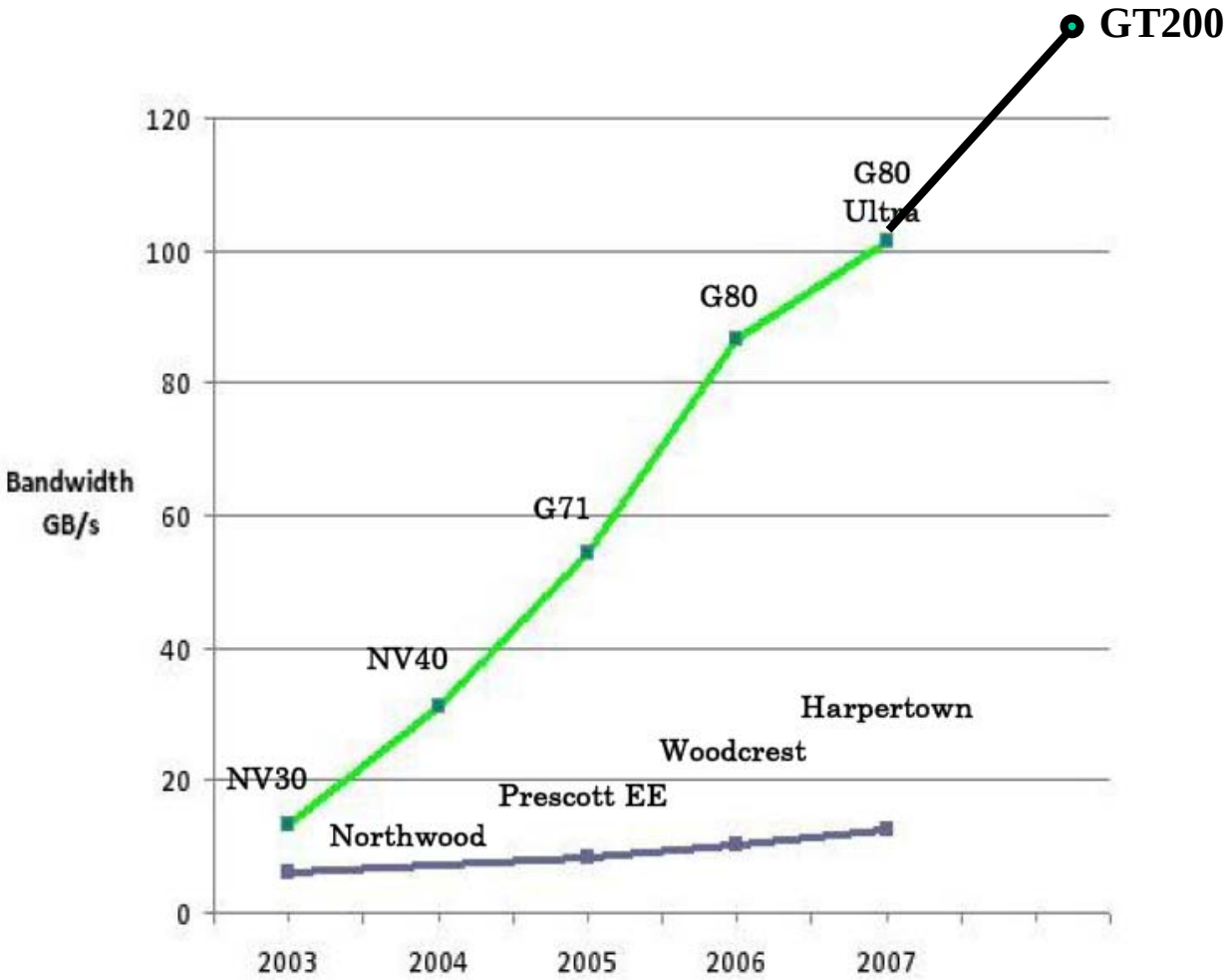
What Speedups Can GPUs Achieve?

- Single-GPU speedups of 8x to 30x vs. CPU core are quite common
- Best speedups (100x!) are attained on codes that are skewed towards floating point arithmetic, esp. CPU-unfriendly operations that prevent effective use of SSE or other vectorization
- Amdahl's Law can prevent legacy codes from achieving peak speedups with only shallow GPU acceleration efforts

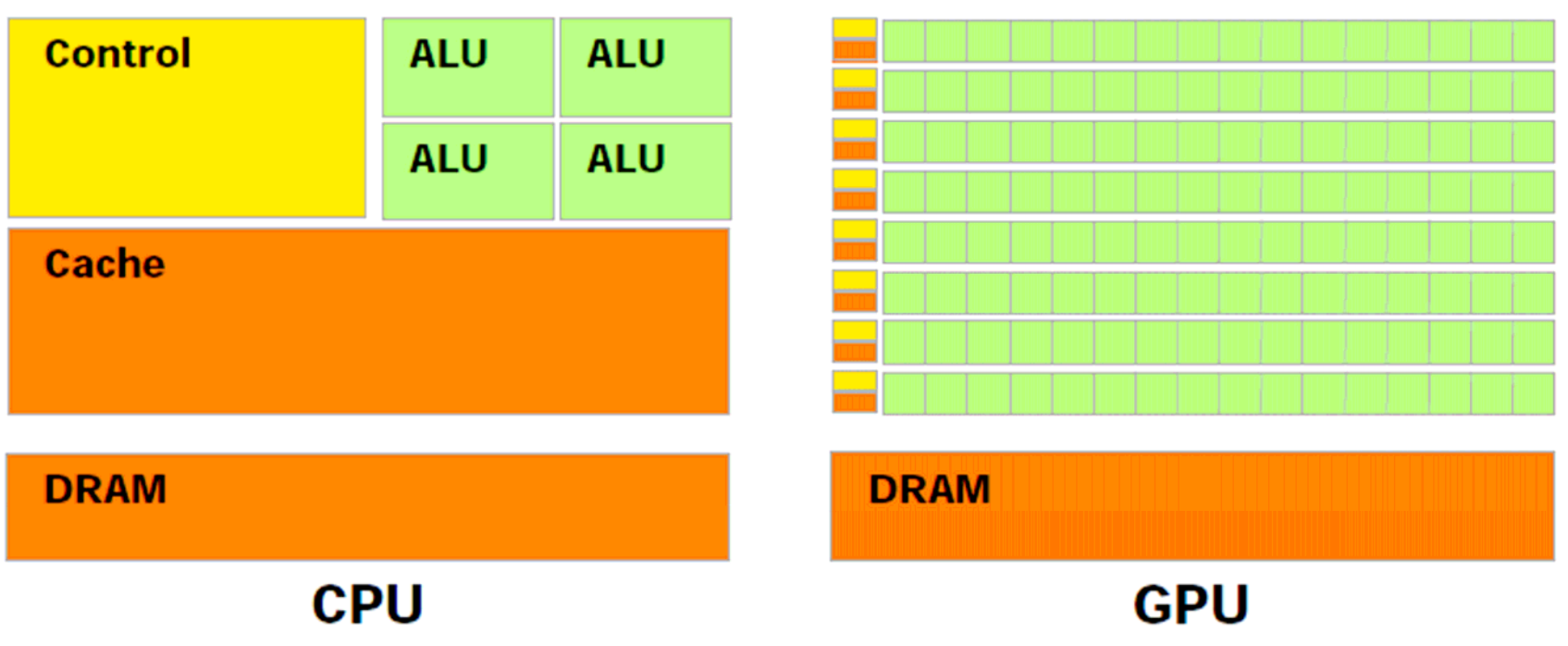
Peak Single-precision Arithmetic Performance Trend

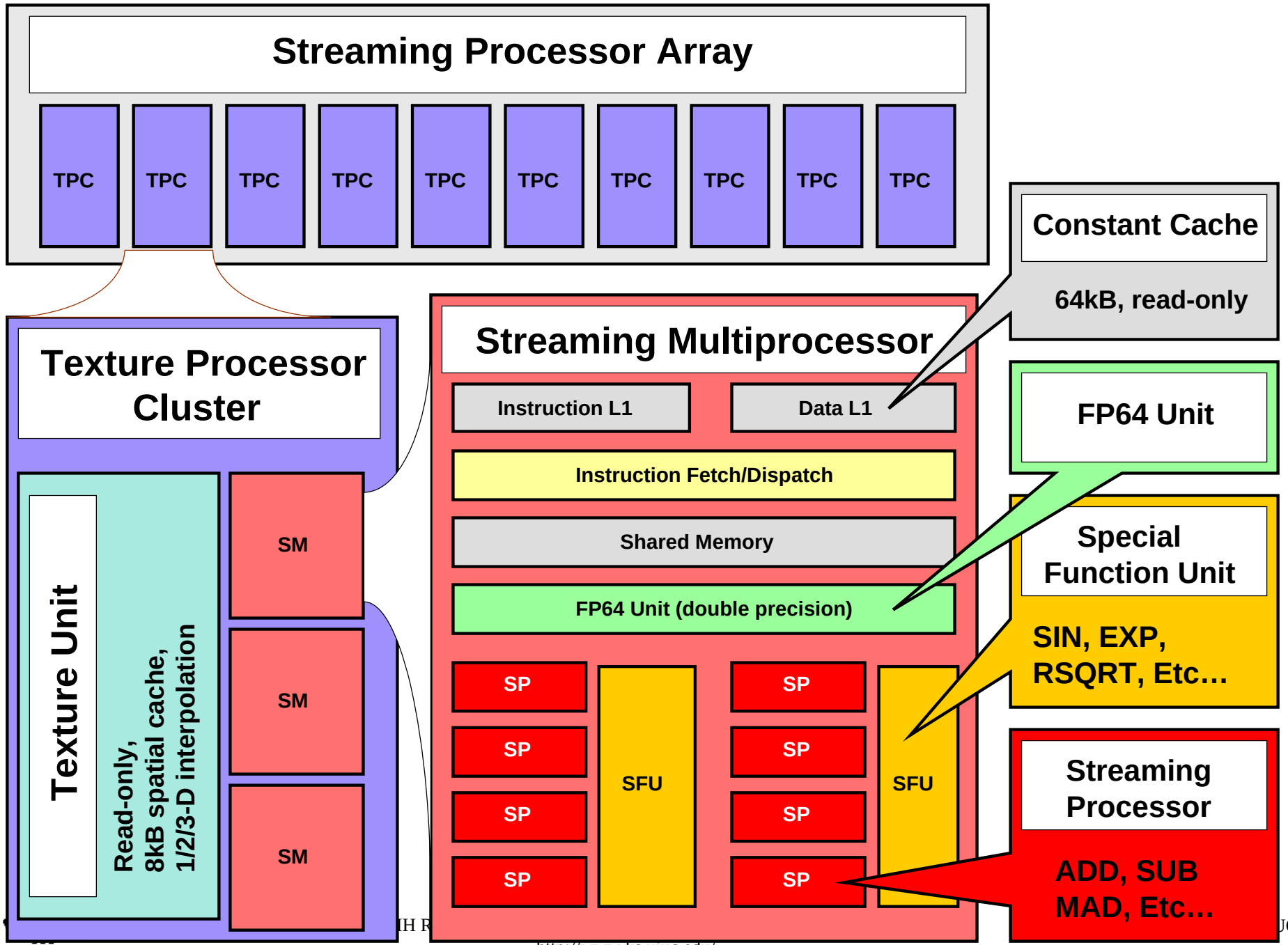


Peak Memory Bandwidth Trend



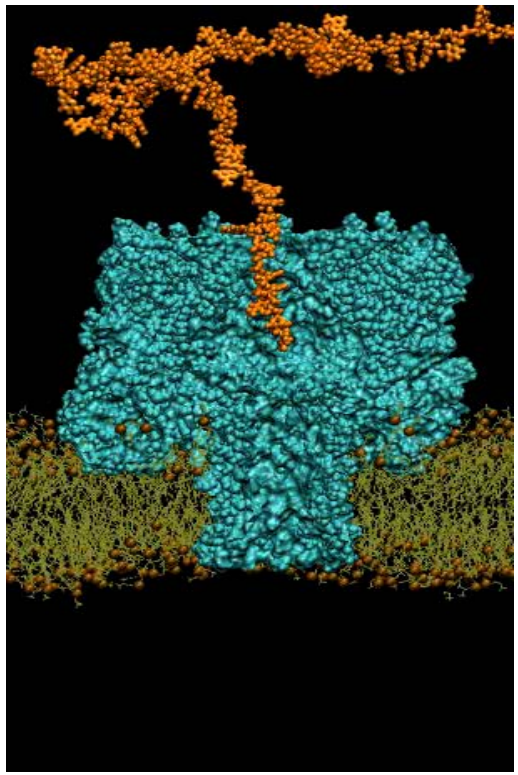
Comparison of CPU and GPU Hardware Architecture




Streaming Processor Array
TPC
TPC
TPC
TPC
TPC
TPC
TPC
TPC
TPC
TPC
Texture Processor Cluster
Texture Unit
Read-only, 8kB spatial cache, 1/2/3-D interpolation
SM
SM
SM
Streaming Multiprocessor
Instruction L1
Data L1
Instruction Fetch/Dispatch
Shared Memory
FP64 Unit (double precision)
SP
SP
SP
SP
SFU
SP
SP
SP
SP
SFU
Constant Cache
64kB, read-only
FP64 Unit
Special Function Unit
SIN, EXP, RSQRT, Etc…
Streaming Processor
ADD, SUB MAD, Etc…

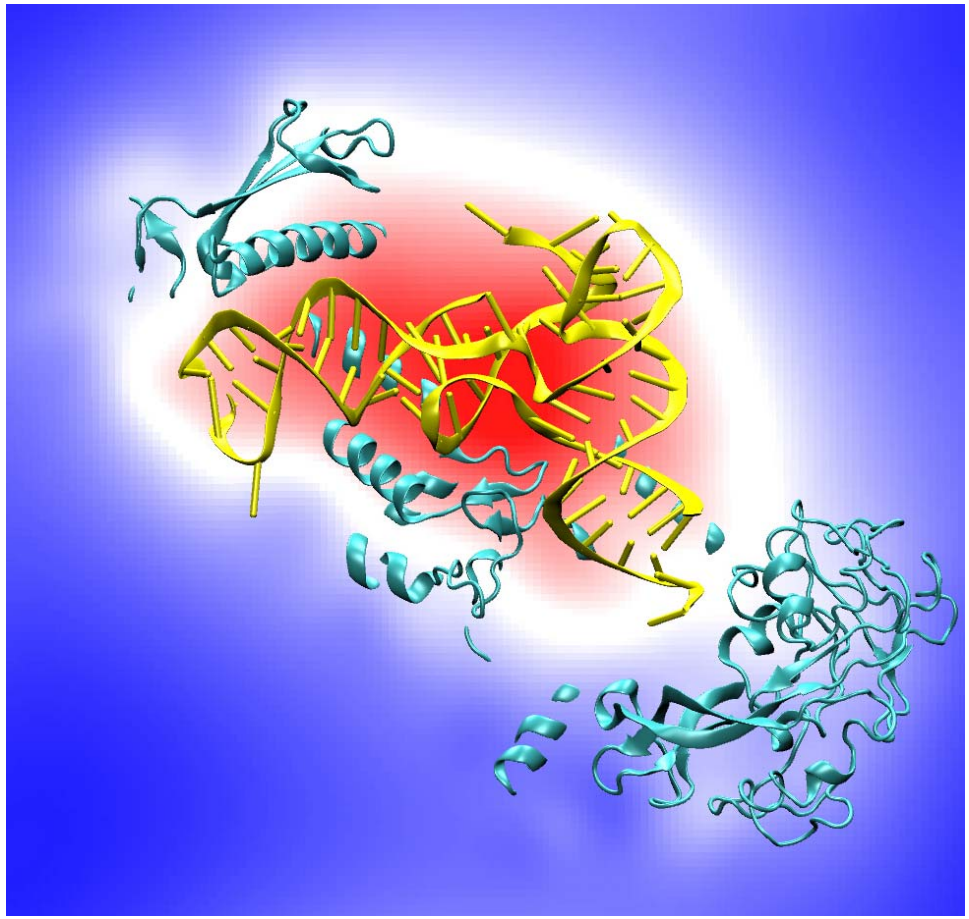
Computational Biology's Insatiable Demand for Processing Power

- Simulations still fall short of biological timescales
- Large simulations extremely difficult to prepare, analyze
- Order of magnitude increase in performance would allow use of more sophisticated models



Calculating Electrostatic Potential Maps

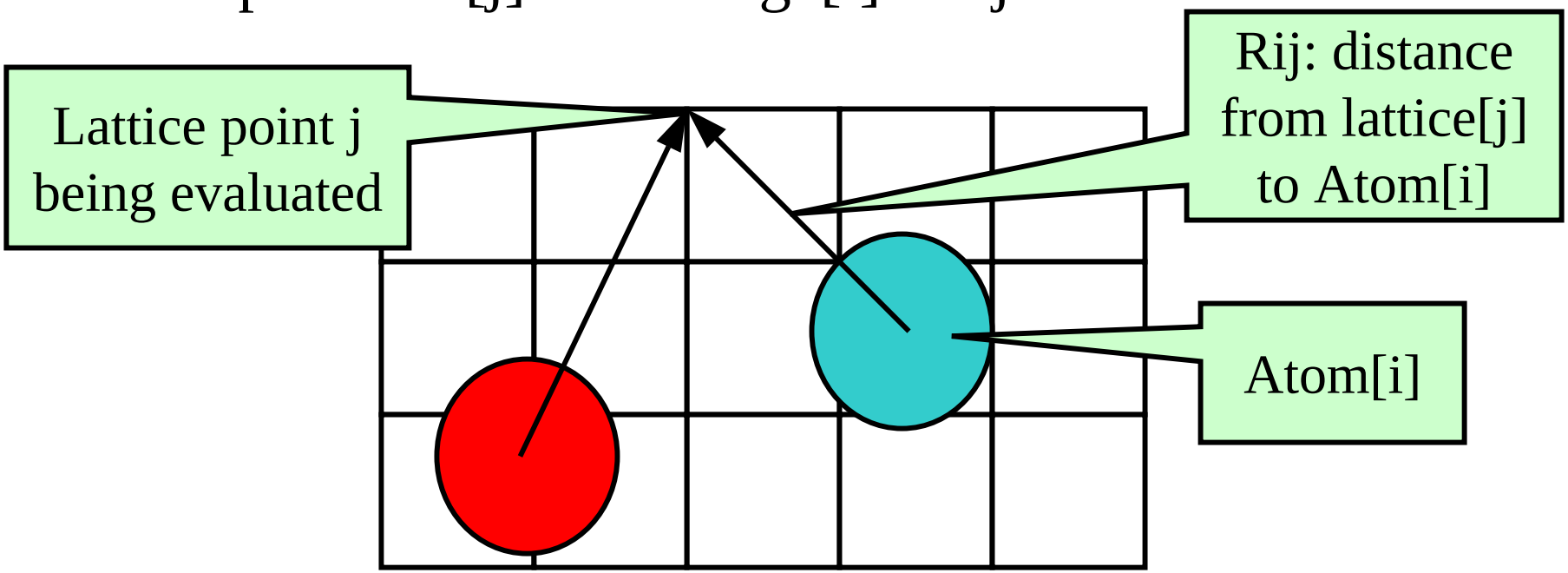
- Used in molecular structure building, analysis, visualization, simulation
- Electrostatic potentials evaluated on a uniformly spaced 3-D lattice
- Each lattice point contains sum of electrostatic contributions of all atoms



Direct Coulomb Summation

- At each lattice point, sum potential contributions for all atoms in the simulated structure:

potential[j] += charge[i] / Rij



DCS Algorithm Design Observations

- Atom list has the smallest memory footprint, best choice for the inner loop (both CPU and GPU)
- Lattice point coordinates are computed on-the-fly
- Atom coordinates are made relative to the origin of the potential map, eliminating redundant arithmetic
- Arithmetic can be significantly reduced by precalculating and reusing distance components, e.g. create a new array containing X, Q, and dy^2 + dz^2, updated on-the-fly for each row (CPU)
- Vectorized CPU versions benefit greatly from SSE instructions

Single Slice DCS: Simple (Slow) C Version

```
void cenergy(float *energygrid, dim3 grid, float gridspacing, float z, const float *atoms, int numatoms) {
  int i,j,n;
  int atomarrdim = numatoms * 4;
  for (j=0; j<grid.y; j++) {
    float y = gridspacing * (float) j;
    for (i=0; i<grid.x; i++) {
      float x = gridspacing * (float) i;
      float energy = 0.0f;
      for (n=0; n<atomarrdim; n+=4) {     // calculate potential contribution of each atom
        float dx = x - atoms[n    ];
        float dy = y - atoms[n+1];
        float dz = z - atoms[n+2];
        energy += atoms[n+3] / sqrtf(dx*dx + dy*dy + dz*dz);
      }
      energygrid[grid.x*grid.y*k + grid.x*j + i] = energy;
    }
  }
```

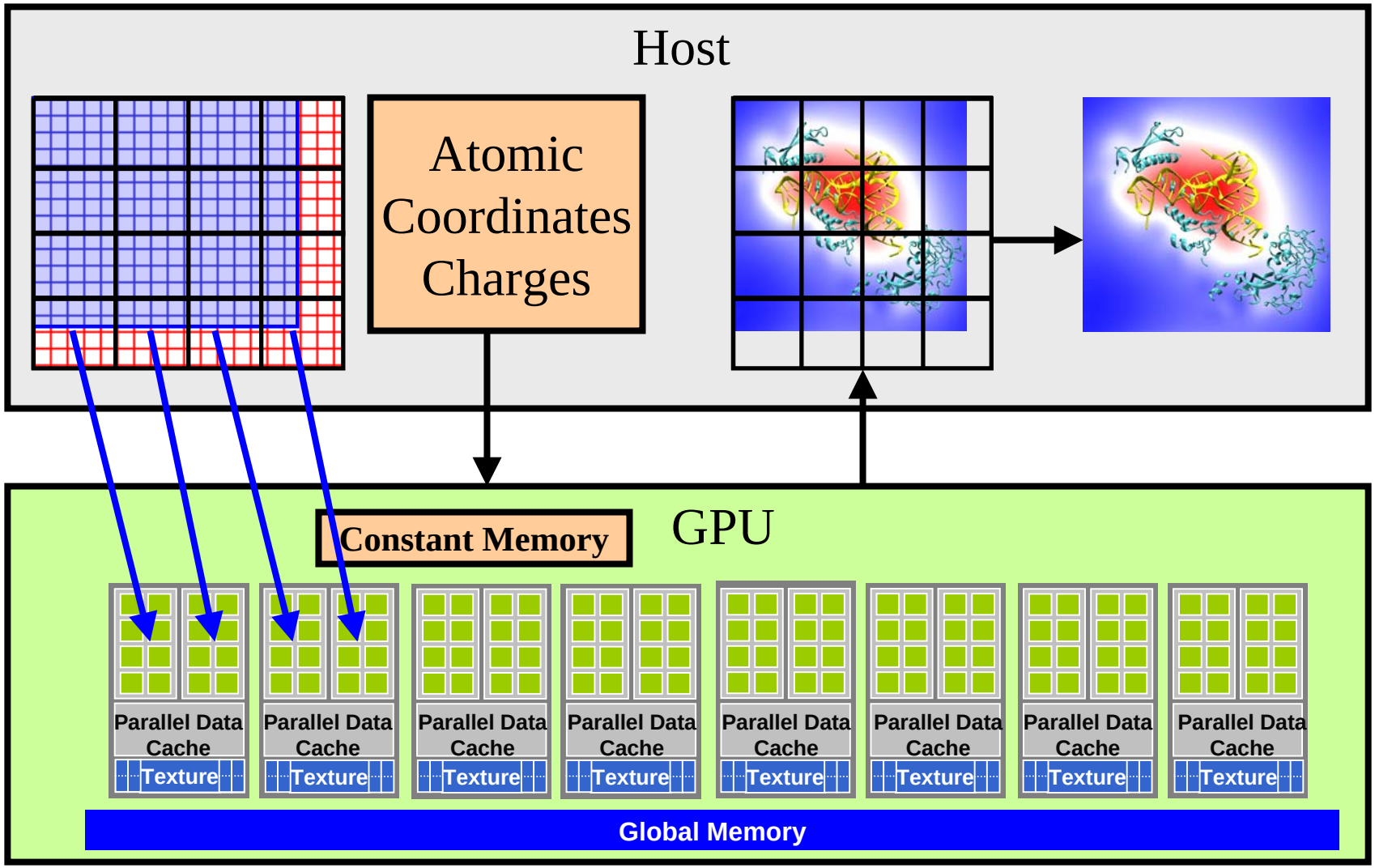
Direct Coulomb Summation on the GPU

- GPU outruns a CPU core by 44x
- Work is decomposed into tens of thousands of independent threads, multiplexed onto hundreds of GPU processing units
- Single-precision FP arithmetic is adequate for intended application
- Numerical accuracy can be further improved by compensated summation, spatially ordered summation groupings, or accumulation of potential in double-precision
- Starting point for more sophisticated algorithms

DCS Observations for GPU Implementation

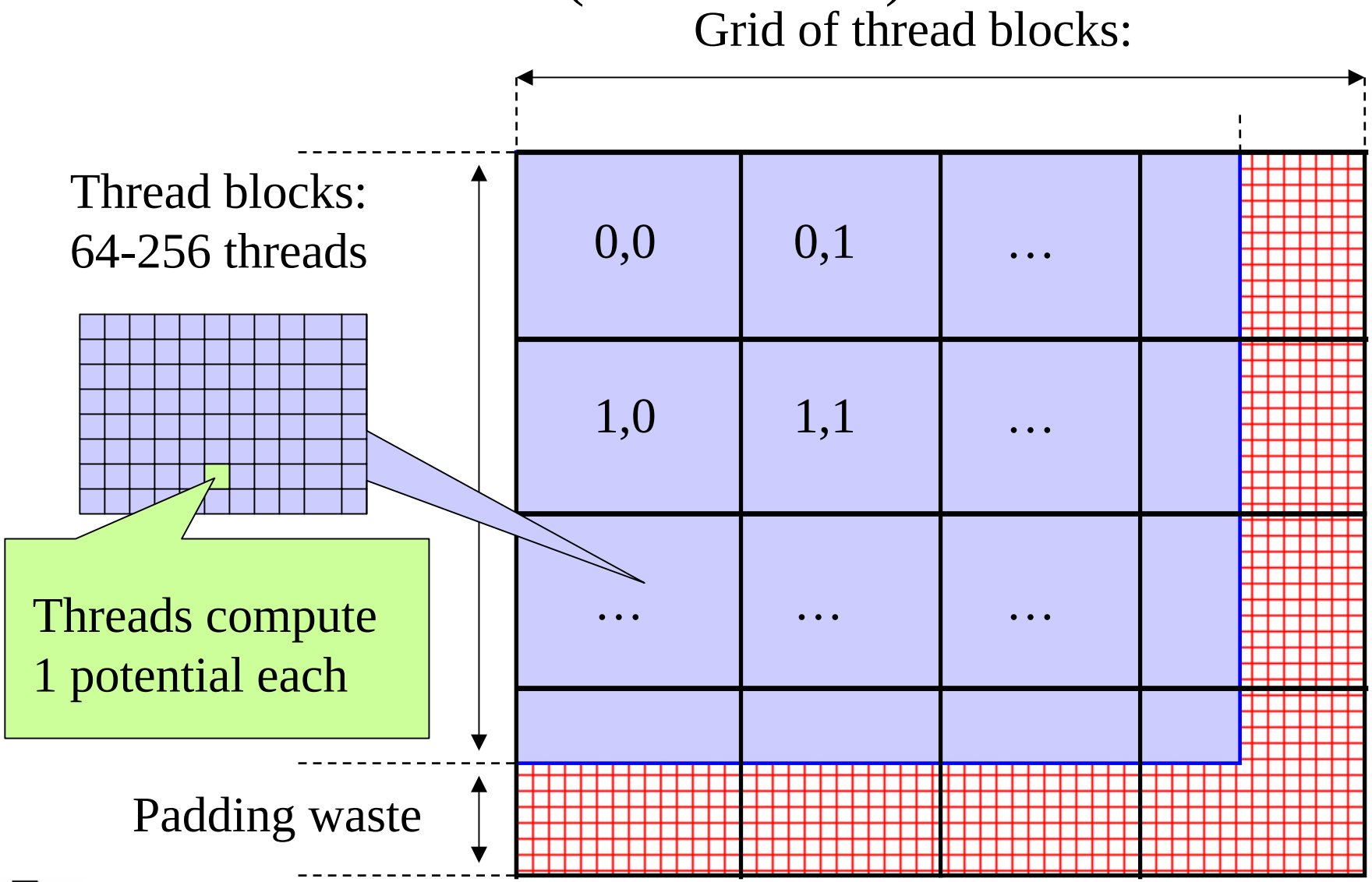
- Straightforward implementation has a low ratio of FLOPS to memory operations (for a GPU…)
- The innermost loop will consume operands VERY quickly
- Since atoms are read-only, they are ideal candidates for texture memory or constant memory
- GPU implementations must access constant memory efficiently, avoid shared memory bank conflicts, and overlap computations with global memory latency
- Map is padded out to a multiple of the thread block size:
  - Eliminates conditional handling at the edges, thus also eliminating the possibility of branch divergence
  - Assists with memory coalescing

Direct Coulomb Summation on the GPU



DCS CUDA Block/Grid Decomposition

(non-unrolled)



DCS Version 1: Const+Precalc
187 GFLOPS, 18.6 Billion Atom Evals/Sec

- Pros:
  - Pre-compute dz^2 for entire slice
  - Inner loop over read-only atoms, const memory ideal
  - If all threads read the same const data at the same time, performance is similar to reading a register
- Cons:
  - Const memory only holds ~4000 atom coordinates and charges
  - Potential summation must be done in multiple kernel invocations per slice, with const atom data updated for each invocation
  - Host must shuffle data in/out for each pass

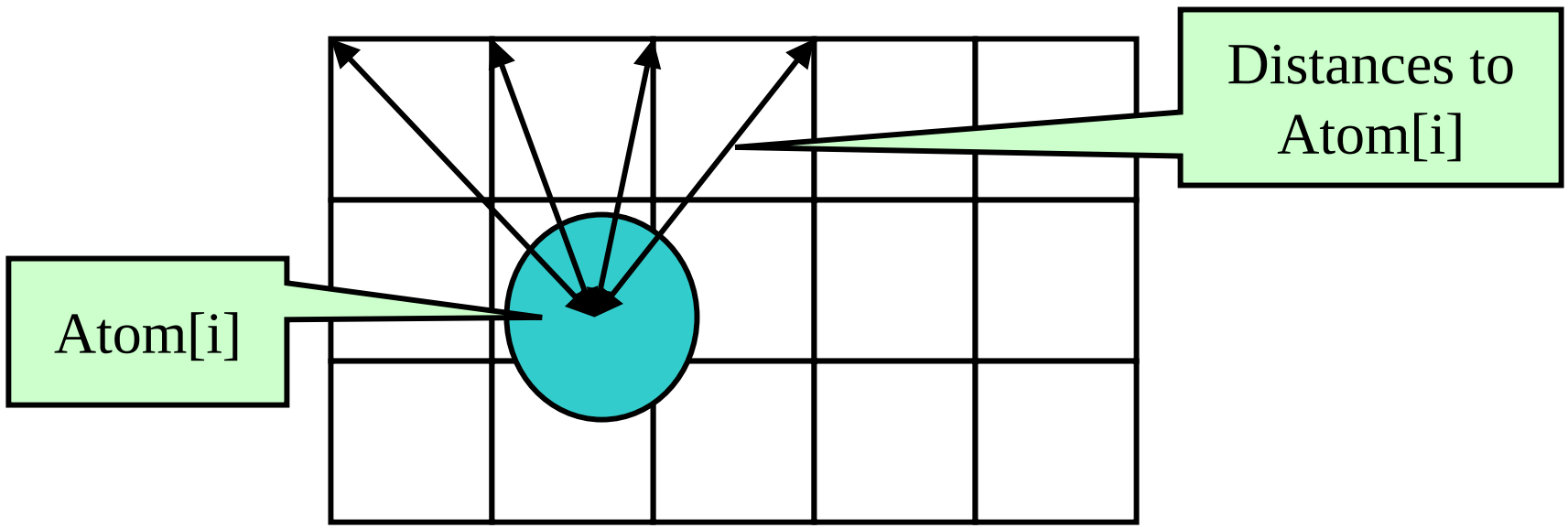
DCS Version 1: Kernel Structure

```
…
  float curenergy = energygrid[outaddr];  // start global mem read very early
  float coorx = gridspacing * xindex;
  float coory = gridspacing * yindex;
  int atomid;
  float energyval=0.0f;

  for (atomid=0; atomid<numatoms; atomid++) {
    float dx = coorx - atominfo[atomid].x;
    float dy = coory - atominfo[atomid].y;
    energyval += atominfo[atomid].w * rsqrtf(dx*dx + dy*dy + atominfo[atomid].z);
  }
  energygrid[outaddr] = curenergy + energyval;
```

DCS CUDA Algorithm: Unrolling Loops

- Reuse atom data and partial distance components multiple times
- Add each atom's contribution to several lattice points at a time, where distances only differ in one component



DCS Inner Loop (Unroll and Jam)

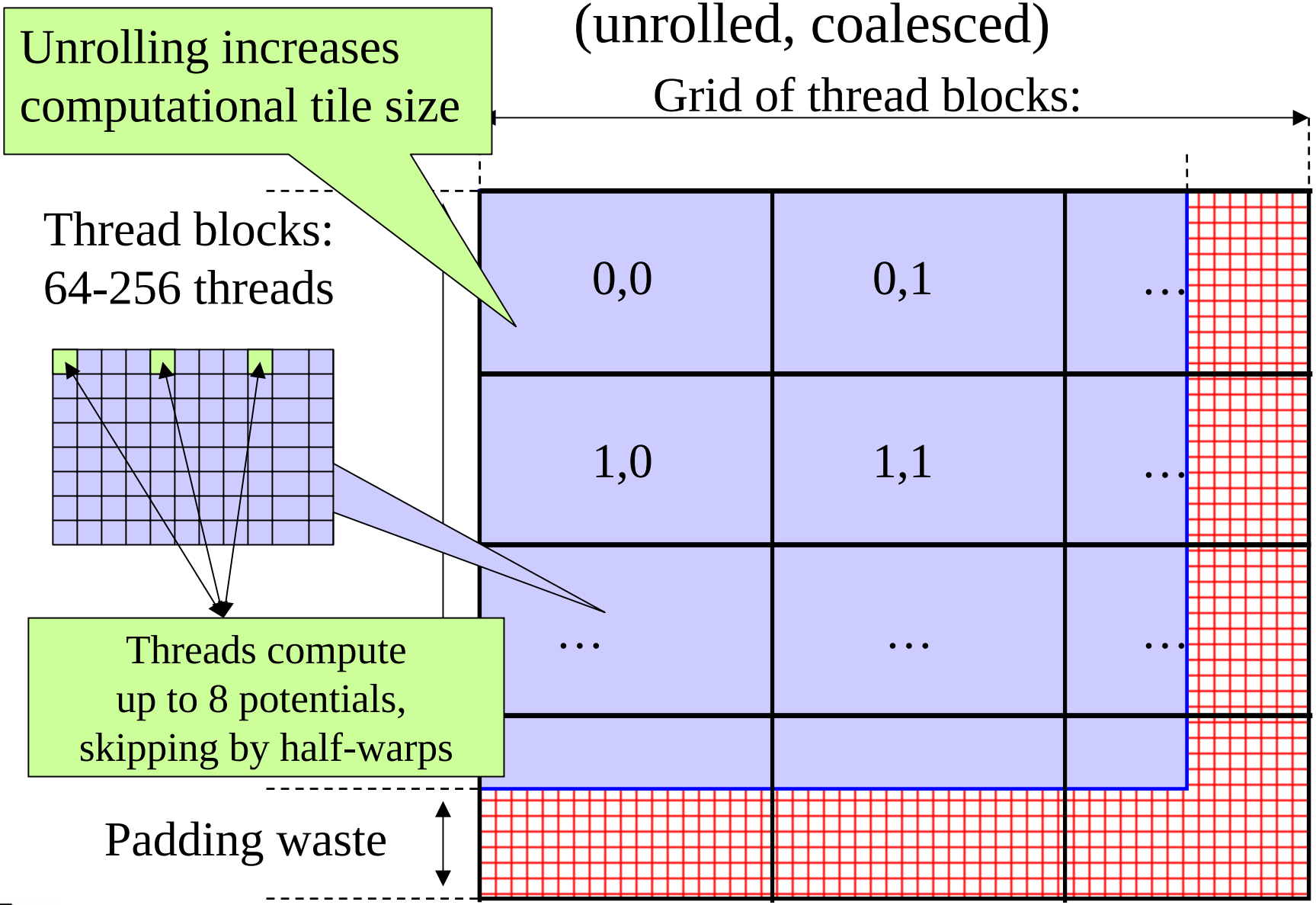
```
…
  for (atomid=0; atomid<numatoms; atomid++) {
    float dy = coory - atominfo[atomid].y;
    float dysqpdzsq = (dy * dy) + atominfo[atomid].z;
    float dx1 = coorx1 - atominfo[atomid].x;
    float dx2 = coorx2 - atominfo[atomid].x;
    float dx3 = coorx3 - atominfo[atomid].x;
    float dx4 = coorx4 - atominfo[atomid].x;
    energyvalx1 += atominfo[atomid].w * rsqrtf(dx1*dx1 + dysqpdzsq);
    energyvalx2 += atominfo[atomid].w * rsqrtf(dx2*dx2 + dysqpdzsq);
    energyvalx3 += atominfo[atomid].w * rsqrtf(dx3*dx3 + dysqpdzsq);
    energyvalx4 += atominfo[atomid].w * rsqrtf(dx4*dx4 + dysqpdzsq);
  }
…
```

DCS CUDA Block/Grid Decomposition (unrolled)

- This optimization technique (unroll and jam) consumes more registers in trade for increased arithmetic intensity
- Kernel variations that calculate more than one lattice point per thread, result in larger computational tiles:
  - Thread count per block must be decreased to reduce computational tile size as unrolling is increased
  - Otherwise, tile size gets bigger as threads do more than one lattice point evaluation, resulting on a significant increase in padding and wasted computations at edges

DCS CUDA Block/Grid Decomposition

(unrolled, coalesced)

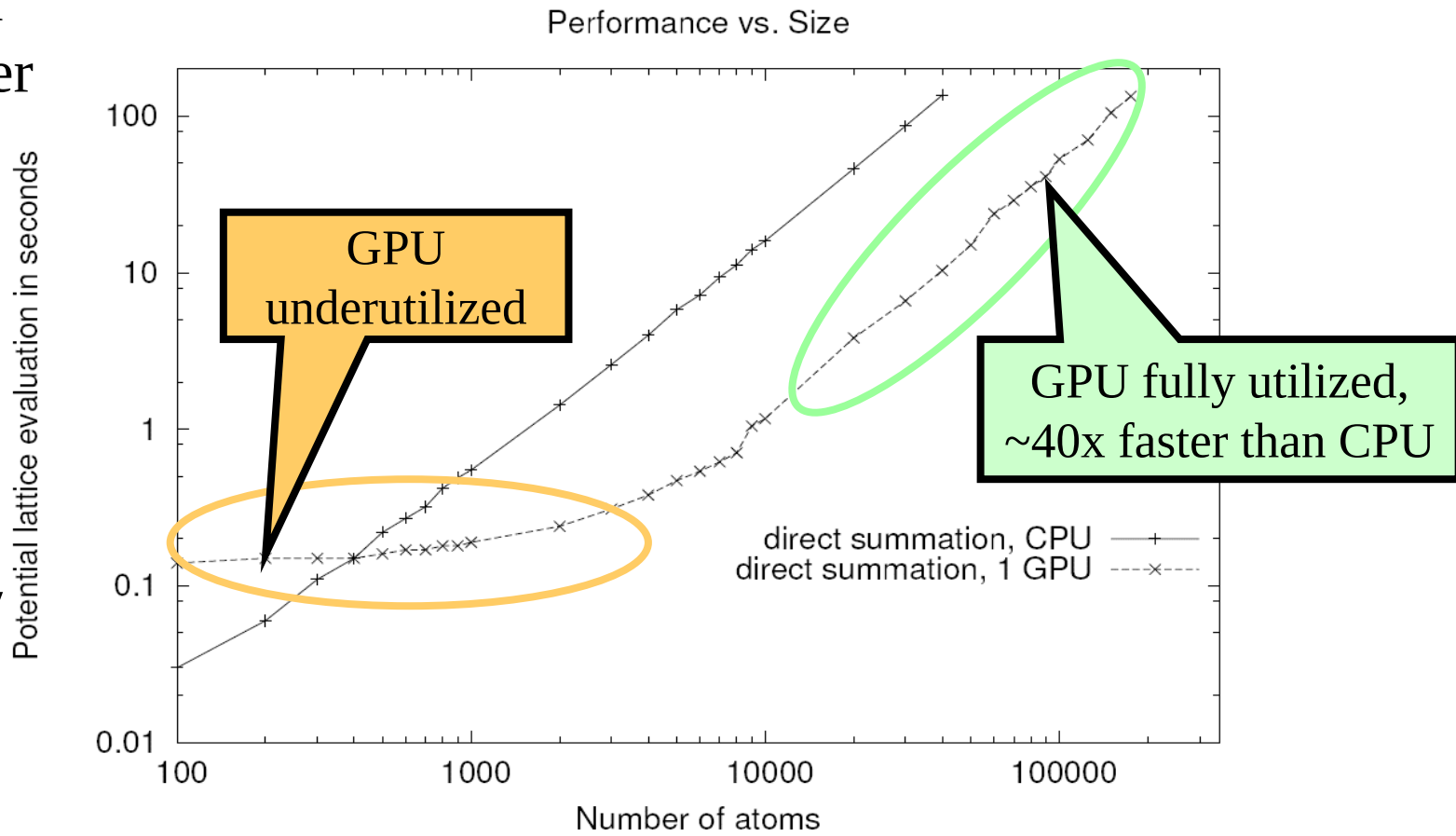


DCS Version 4: Kernel Structure
291.5 GFLOPS, 39.5 Billion Atom Evals/Sec

- Processes 8 lattice points at a time in the inner loop
- Subsequent lattice points computed by each thread are offset to guarantee coalesced memory accesses
- Loads and increments 8 potential map lattice points from global memory at completion of of the summation, avoiding register consumption
- Code is too long to show, but is available by request

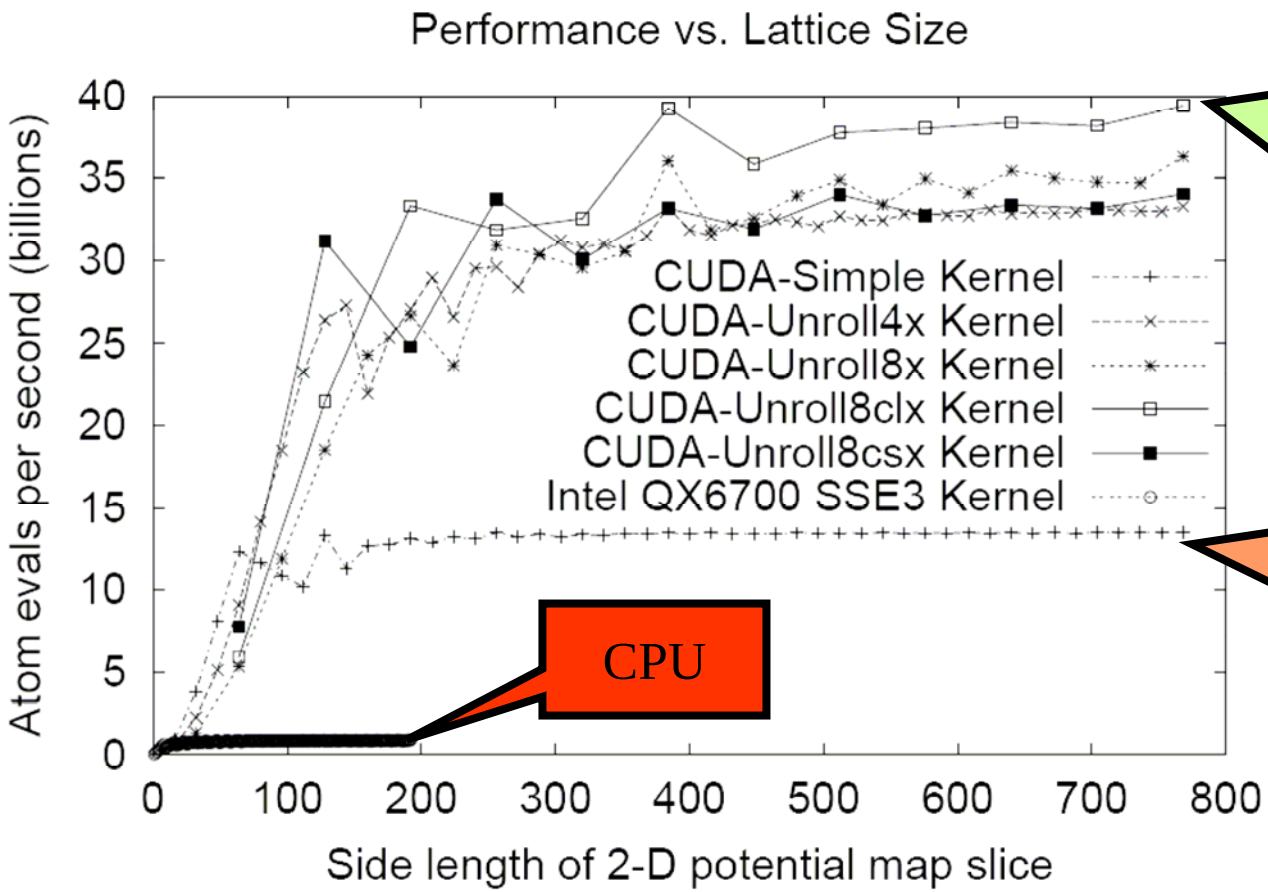
Direct Coulomb Summation Runtime

Lower is better



Accelerating molecular modeling applications with graphics processors. J. Stone, J. Phillips, P. Freddolino, D. Hardy, L. Trabuco, K. Schulten. *J. Comp. Chem.*, 28:2618-2640, 2007.

Direct Coulomb Summation Performance



CUDA-Unroll8clx: fastest GPU kernel, 44x faster than CPU, 291 GFLOPS on GeForce 8800GTX

CUDA-Simple: 14.8x faster, 33% of fastest GPU kernel

GPU computing. J. Owens, M. Houston, D. Luebke, S. Green, J. Stone, J. Phillips. *Proceedings of the IEEE*, 96:879-899, 2008.

Multi-GPU DCS Algorithm:

- One host thread is created for each CUDA GPU, attached according to host thread ID:
  - First CUDA call binds that thread's CUDA context to that GPU for life
- Map slices are decomposed cyclically onto the available GPUs
- Map slices are usually larger than the host memory page size, so false sharing and related effects are not a problem for this application

Multi-GPU Direct Coulomb Summation

- Effective memory bandwidth scales with the number of GPUs utilized
- PCIe bus bandwidth not a bottleneck for this algorithm
- 117 billion evals/sec
- 863 GFLOPS
- 131x speedup vs. CPU core
- Power: 700 watts during benchmark

Quad-core Intel QX6700

Three NVIDIA GeForce 8800GTX

Multi-GPU Direct Coulomb Summation

- 4-GPU (2 Quadroplex) Opteron node at NCSA
- 157 billion evals/sec
- 1.16 TFLOPS
- 176x speedup vs. Intel QX6700 CPU core w/ SSE

- 4-GPU GTX 280 (GT200)
- 241 billion evals/sec
- 1.78 TFLOPS
- 271x speedup vs. Intel QX6700 CPU core w/ SSE

NCSA GPU Cluster

http://www.ncsa.uiuc.edu/Projects/GPUcluster/

Infinite vs. Cutoff Potentials

- Infinite range potential:
  - All atoms contribute to all lattice points
  - Summation algorithm has quadratic complexity
- Cutoff (range-limited) potential:
  - Atoms contribute within cutoff distance to lattice points
  - Summation algorithm has linear time complexity
  - Has many applications in molecular modeling:
    - Replace electrostatic potential with shifted form
    - Short-range part for fast methods of approximating full electrostatics
    - Used for fast decaying interactions (e.g. Lennard-Jones, Buckingham)

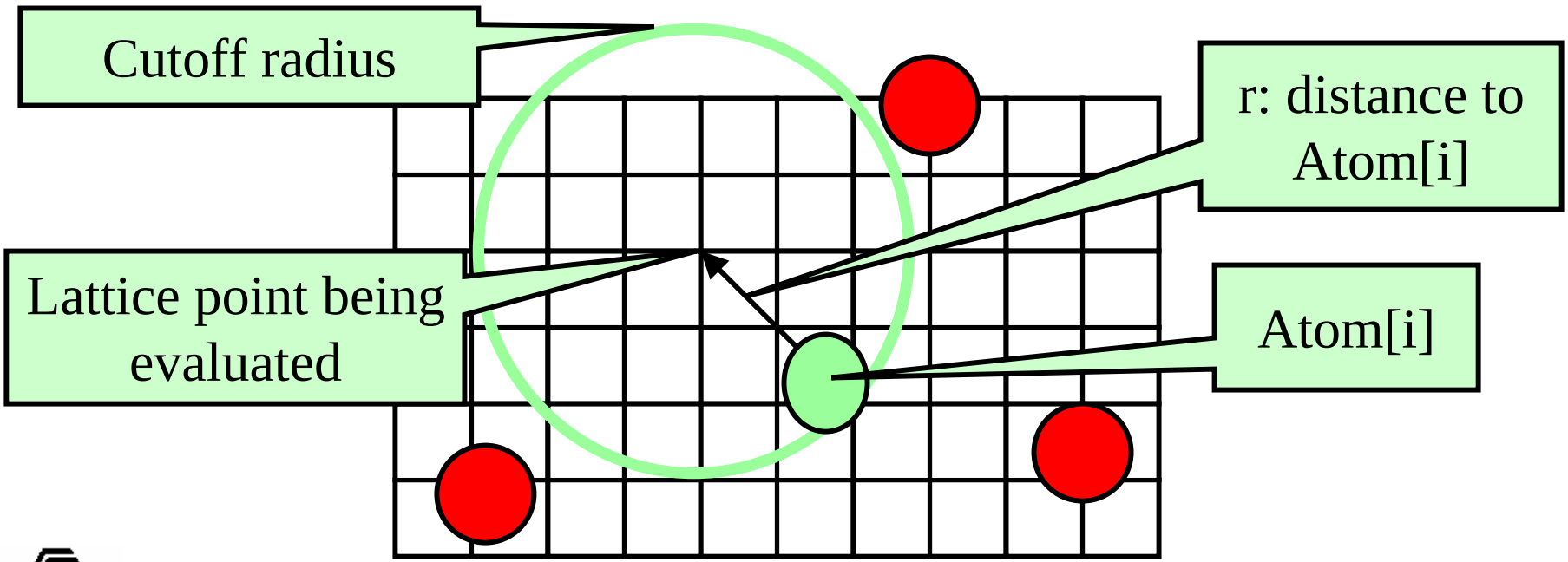
Cutoff Summation

- At each lattice point, sum potential contributions for atoms within cutoff radius:

  if (distance to atom[i] < cutoff)

    potential += (charge[i] / r) * s(r)

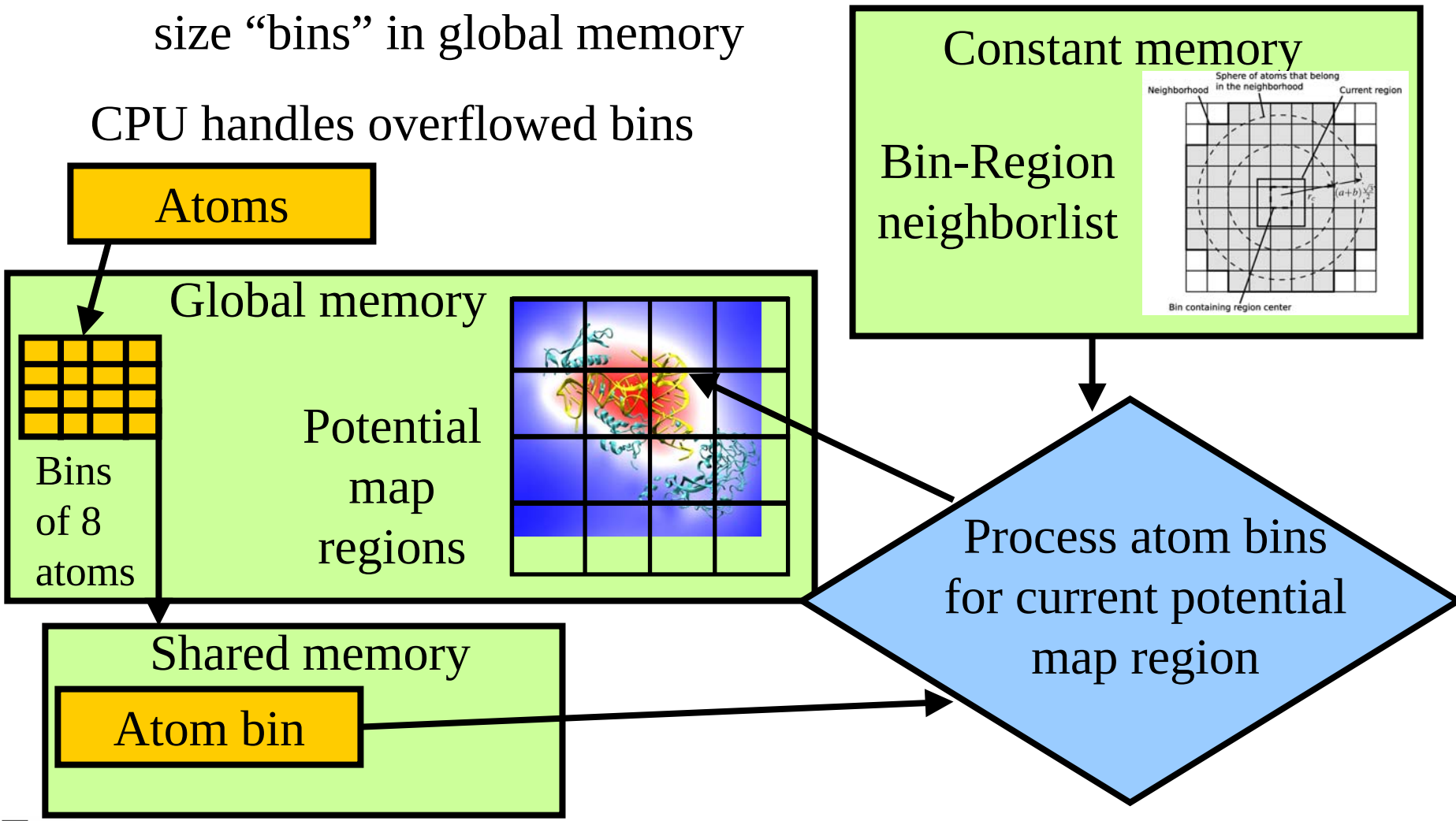
- Smoothing function s(r) is algorithm dependent



Cutoff Summation on the GPU

Atoms spatially hashed into fixed-size “bins” in global memory

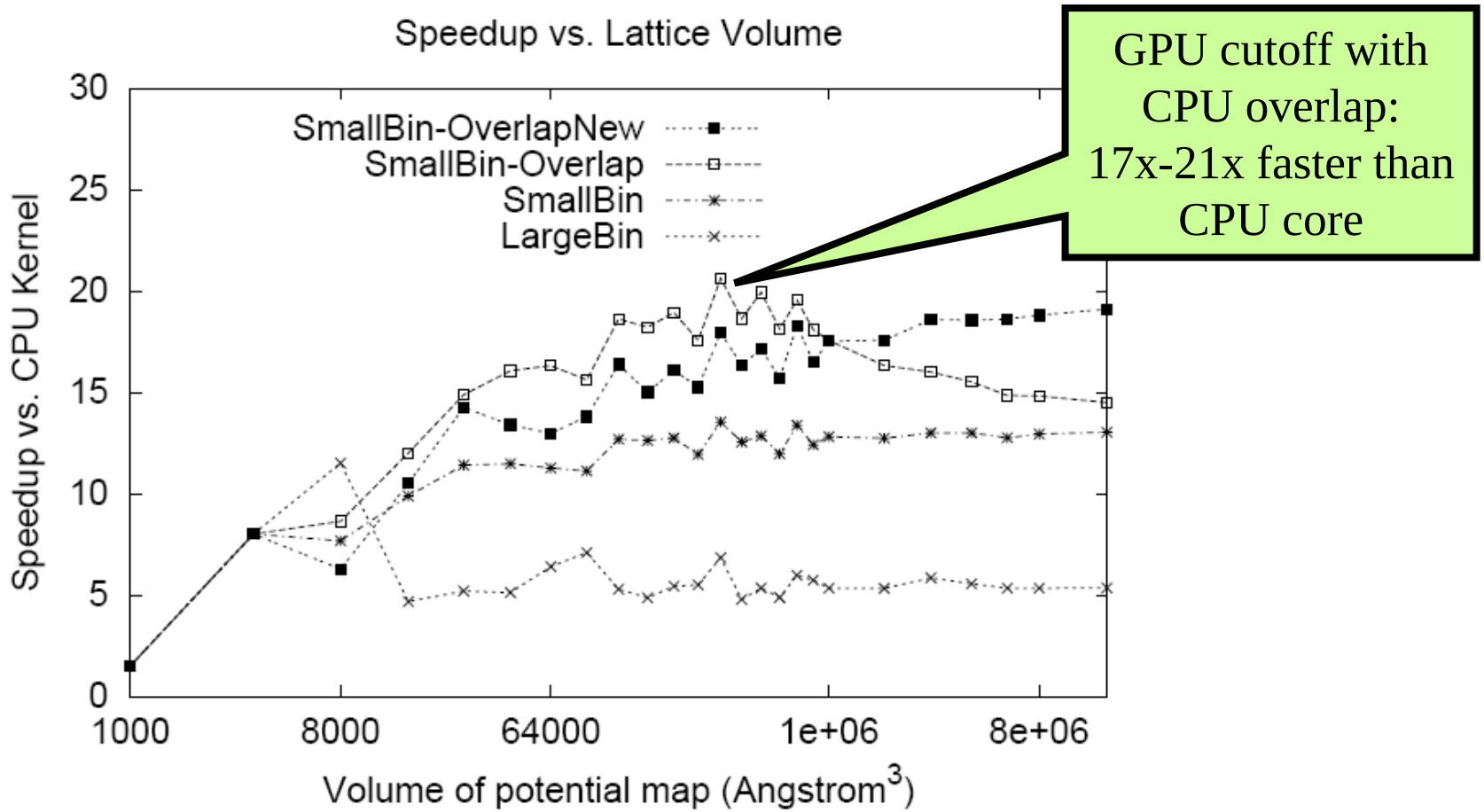
CPU handles overflowed bins



Using the CPU to Improve GPU Performance

- GPU performs best when the work evenly divides into the number of threads/processing units
- Optimization strategy:
  - Use the CPU to “regularize” the GPU workload
  - Handle exceptional or irregular work units on the CPU while the GPU processes the bulk of the work
  - On average, the GPU is kept highly occupied, attaining a much higher fraction of peak performance

Cutoff Summation Runtime



GPU acceleration of cutoff pair potentials for molecular modeling applications. C. Rodrigues, D. Hardy, J. Stone, K. Schulten, W. Hwu. *Proceedings of the 2008 Conference On Computing Frontiers*, pp. 273-282, 2008.

NAMD Parallel Molecular Dynamics

Kale et al., J. Comp. Phys. 151:283-312, 1999.

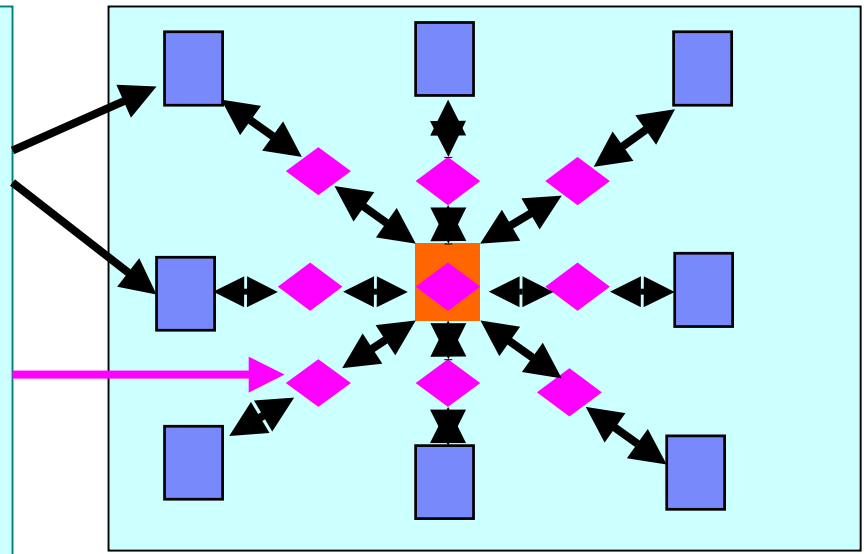
- Designed from the beginning as a parallel program
- Uses the Charm++ philosophy:
  - Decompose computation into a large number of objects
  - Intelligent Run-time system (Charm++) assigns objects to processors for dynamic load balancing with minimal communication

Hybrid of spatial and force decomposition:

•Spatial decomposition of atoms into cubes (called patches)

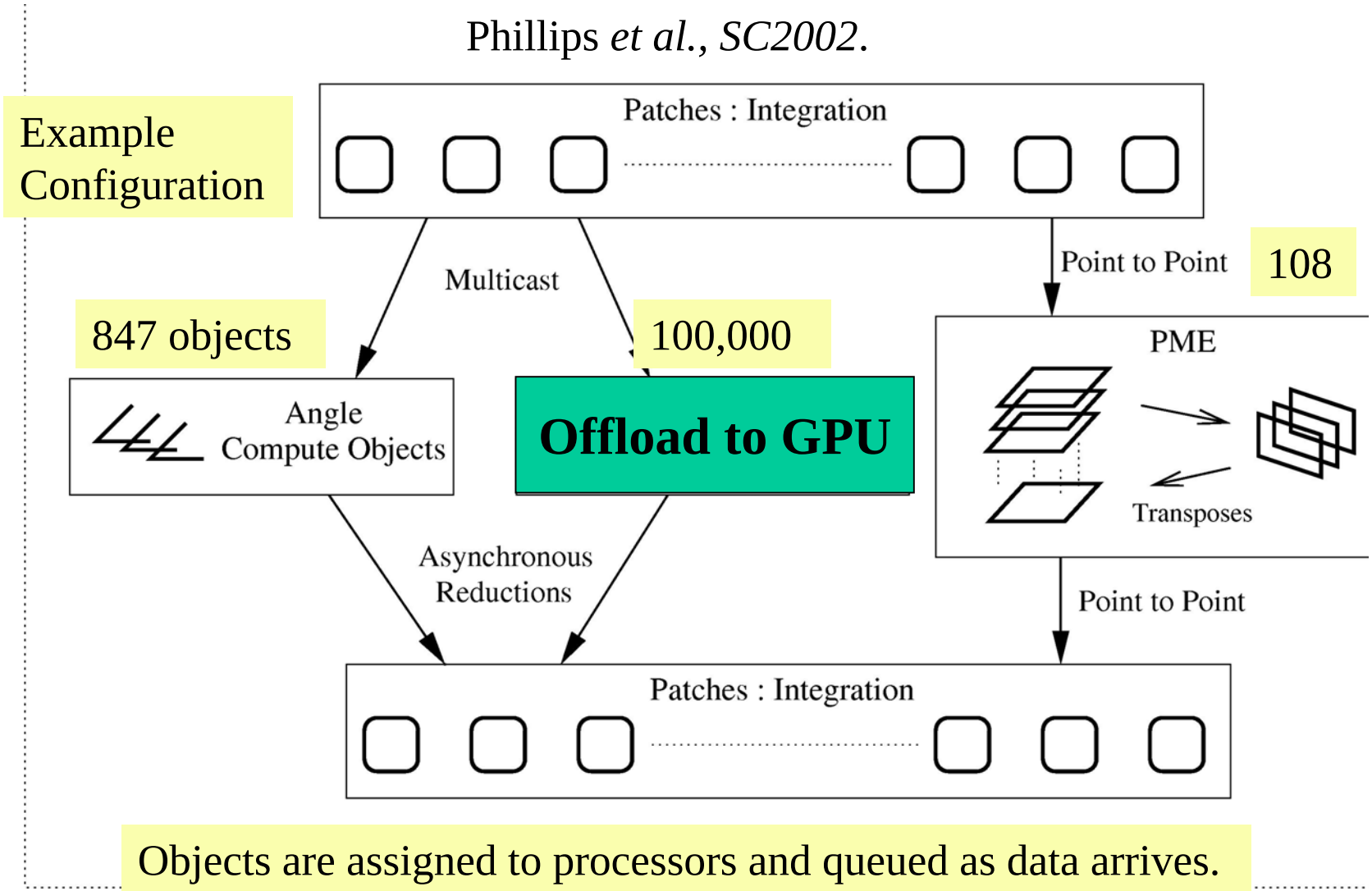
•For every pair of interacting patches, create one object for calculating electrostatic interactions

•Recent: Blue Matter, Desmond, etc. use this idea in some form



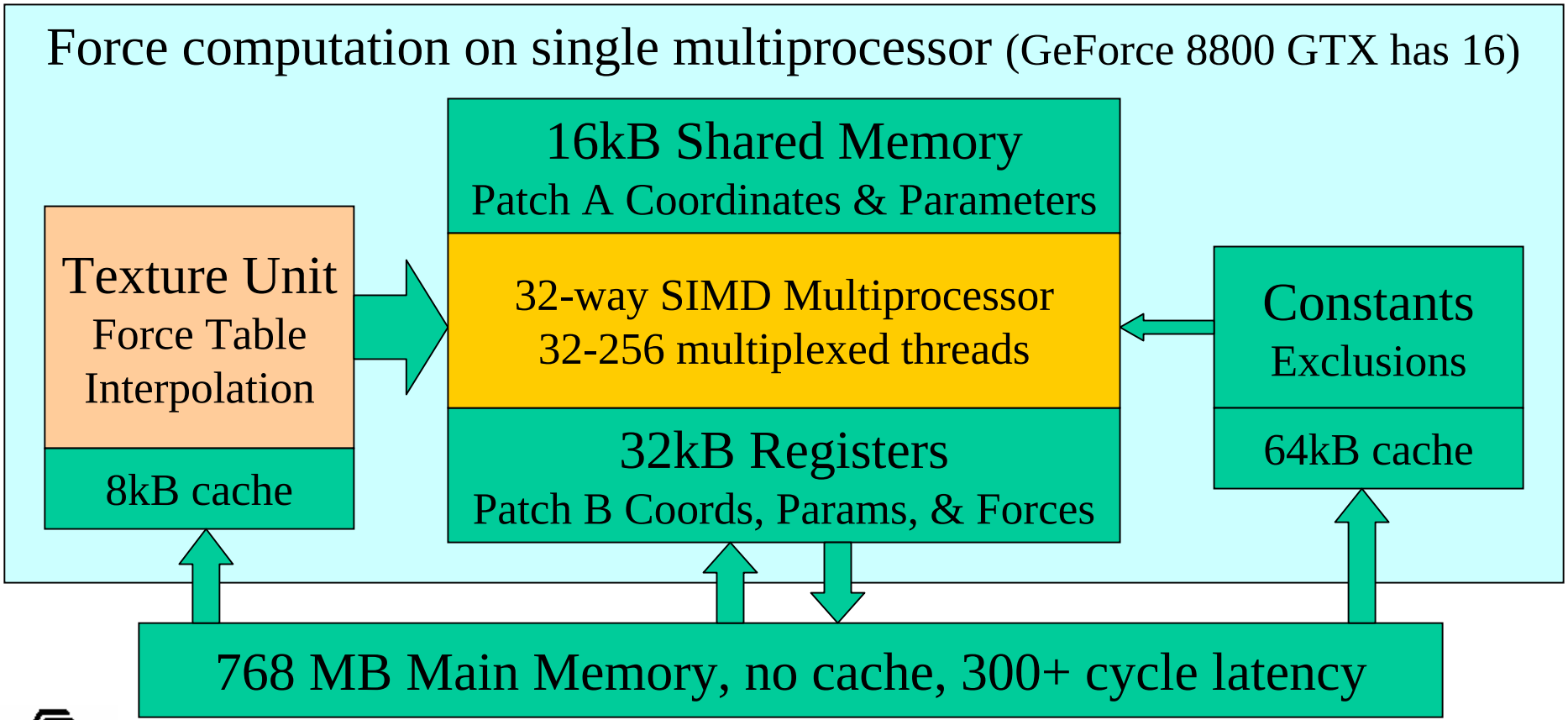
NAMD Overlapping Execution

Phillips *et al.*, *SC2002*.



Nonbonded Forces on G80 GPU

- Start with most expensive calculation: direct nonbonded interactions.
- Decompose work into pairs of patches, identical to NAMD structure.
- GPU hardware assigns patch-pairs to multiprocessors dynamically.



Stone *et al.*, *J. Comp. Chem.* **28**:2618-2640, 2007.

Nonbonded Forces CUDA Code

```
texture<float4> force_table;
__constant__ unsigned int exclusions[];
__shared__ atom jatom[];
atom iatom;      // per-thread atom, stored in registers
float4 iforce;   // per-thread force, stored in registers
for ( int j = 0; j < jatom_count; ++j ) {
  float dx = jatom[j].x - iatom.x;   float dy = jatom[j].y - iatom.y;  float dz = jatom[j].z - iatom.z;
  float r2 = dx*dx + dy*dy + dz*dz;
  if ( r2 < cutoff2 ) {
    float4 ft = texfetch(force_table, 1.f/sqrt(r2));
    bool excluded = false;
    int indexdiff = iatom.index - jatom[j].index;
    if ( abs(indexdiff) <= (int) jatom[j].excl_maxdiff ) {
      indexdiff += jatom[j].excl_index;
      excluded = ((exclusions[indexdiff>>5] & (1<<(indexdiff&31))) != 0);
    }
    float f = iatom.half_sigma + jatom[j].half_sigma;  // sigma
    f *= f*f;  // sigma^3
    f *= f;  // sigma^6
    f *= ( f * ft.x + ft.y );  // sigma^12 * fi.x - sigma^6 * fi.y
    f *= iatom.sqrt_epsilon * jatom[j].sqrt_epsilon;
    float qq = iatom.charge * jatom[j].charge;
    if ( excluded ) { f = qq * ft.w; }  // PME correction
    else { f += qq * ft.z; }  // Coulomb
    iforce.x += dx * f;   iforce.y += dy * f;    iforce.z += dz * f;
    iforce.w += 1.f;  // interaction count or energy
  }
}
```

Force Interpolation

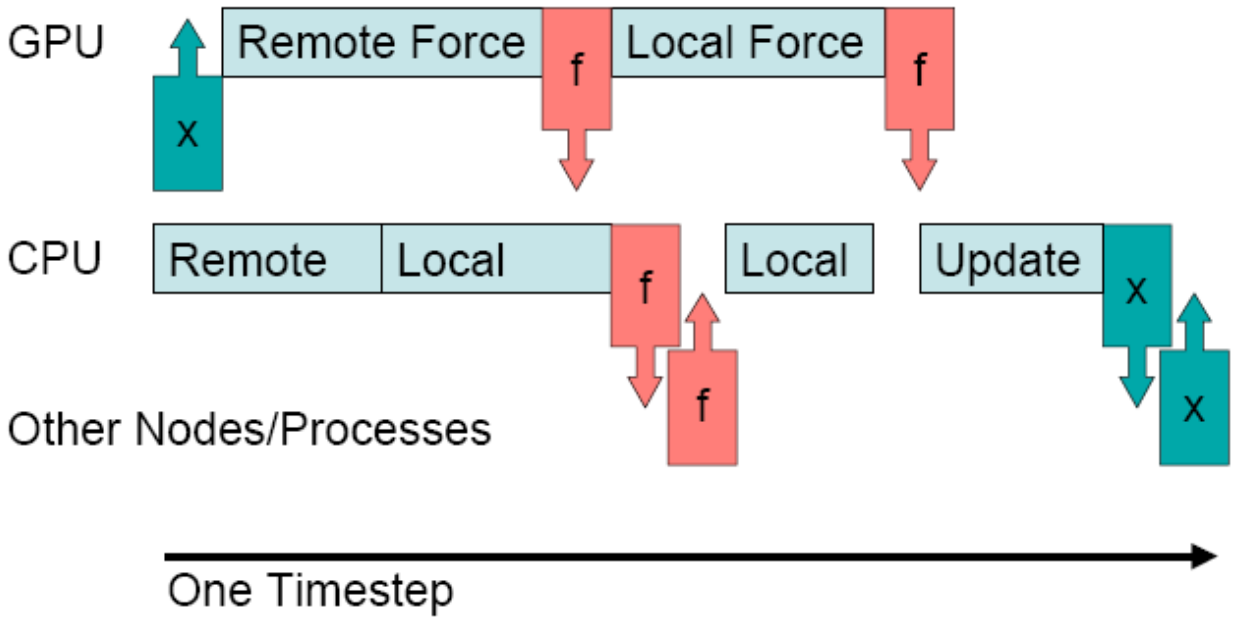
Exclusions

Parameters

Accumulation

Stone *et al.*, *J. Comp. Chem.* **28**:2618-2640, 2007.

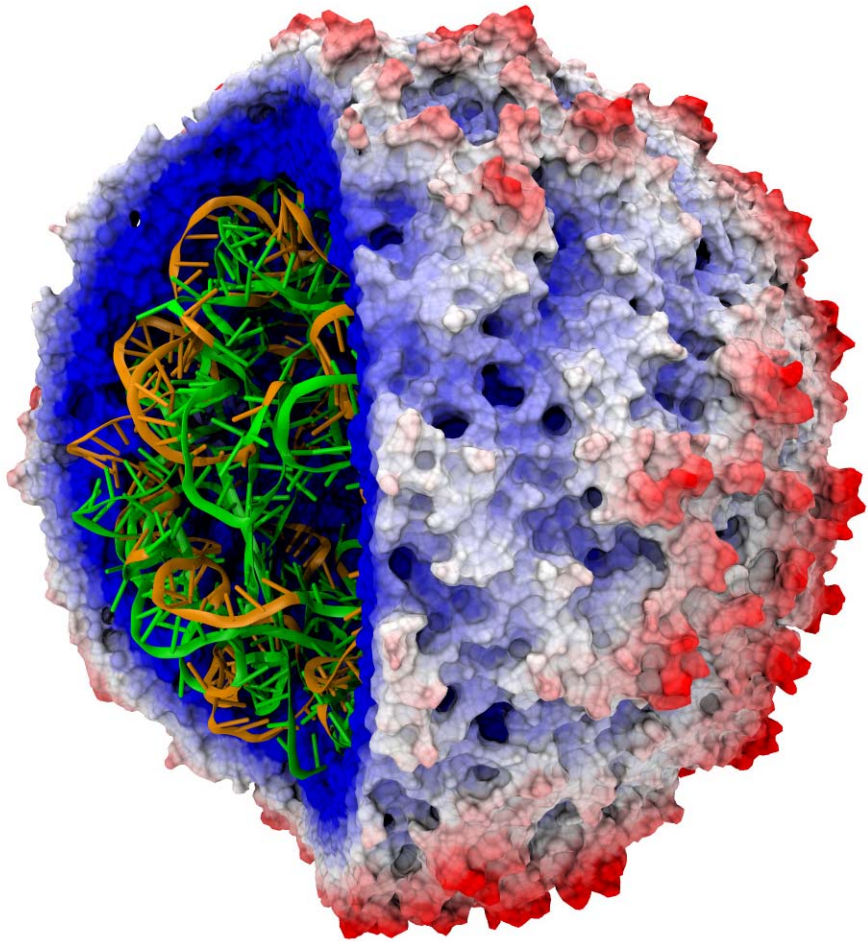
NAMD Overlapping Execution with Asynchronous CUDA kernels



GPU kernels are launched asynchronously, CPU continues with its own work, polling for GPU completion periodically. Forces needed by remote nodes are explicitly scheduled to be computed ASAP to improve overall performance.

Molecular Simulations: Virology

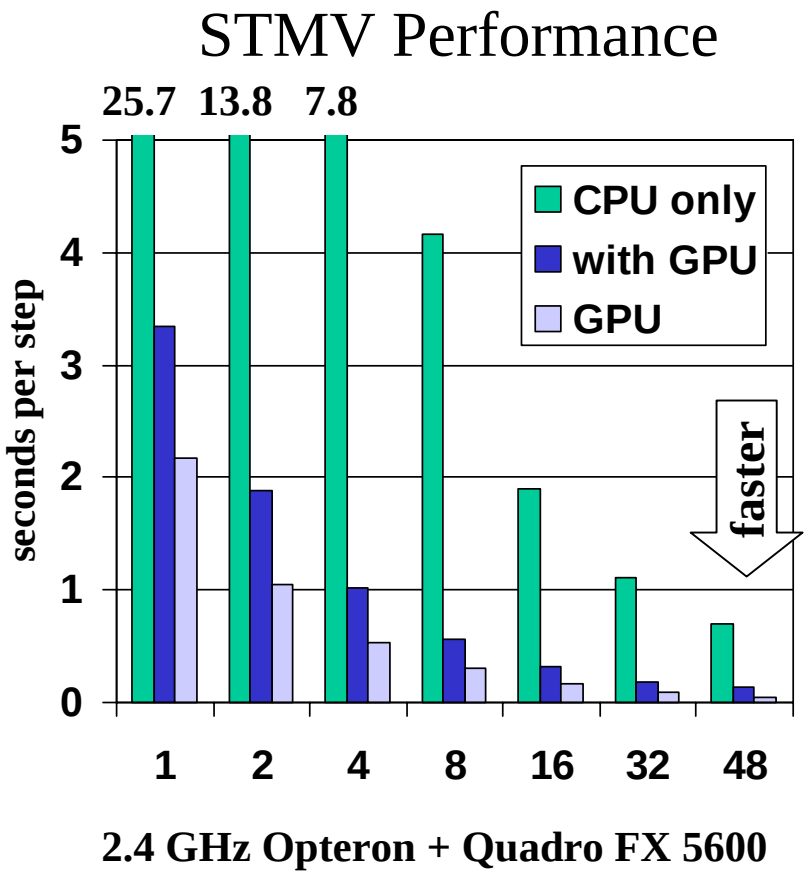
- Simulations lead to better understanding of the mechanics of viral infections
- Better understanding of infection mechanics at the molecular level may result in more effective treatments for diseases
- Since viruses are large, their computational “viewing” requires tremendous resources, in particular large parallel computers
- GPUs can significantly accelerate the simulation, analyses, and visualization of such structures



Satellite Tobacco Mosaic Virus (STMV)

NAMD Performance on NCSA GPU Cluster, April 2008

- STMV virus (1M atoms)
- 60 GPUs match performance of 330 CPU cores
- 5.5-7x overall application speedup w/ G80-based GPUs
- Overlap with CPU
- Off-node results done first
- Plans for better performance
  - Tune or port remaining work
  - Balance GPU load



NAMD Performance on NCSA GPU Cluster, April 2008

CPU Cores & GPUs	4	8	16	32	60
GPU-accelerated performance					
Local blocks/GPU	13186	5798	2564	1174	577
Remote blocks/GPU	1644	1617	1144	680	411
GPU s/step	0.544	0.274	0.139	0.071	0.040
Total s/step	0.960	0.483	0.261	0.154	0.085
Unaccelerated performance					
Total s/step	6.76	3.33	1.737	0.980	0.471
Speedup from GPU acceleration					
Factor	7.0	6.9	6.7	6.4	5.5

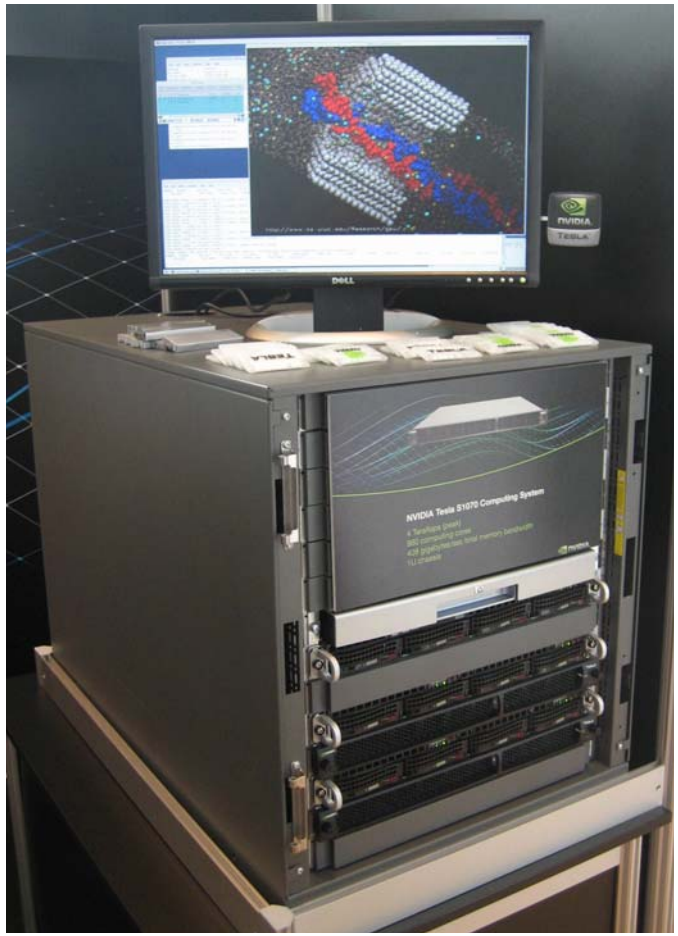
STMV benchmark, 1M atoms,12A cutoff, PME every 4 steps, on 2.4 GHz AMD Opteron + NVIDIA Quadro FX 5600

General GPU Clustering Issues
(As of November 2008)

- Tremendous increase in compute capability per node places higher demands on the InfiniBand interconnect
- Exchanging data between GPUs on the same node currently requires involvement of the host and multiple copy operations
- No industry standard for user-mode DMA in message passing and accelerator APIs:
  - Example: Use of InfiniBand RDMA (even indirectly by the MPI library) can conflict with CUDA's pinned memory APIs, causing deadloock
  - No support for direct RDMA to/from GPUs, all incoming/outgoing RDMAs for the GPU involve extra copies to the host

NAMD Performance on GT200 GPU Cluster, August 2008

- 8 GT200s, 240 SPs @ 1.3GHz:
  - 72x faster than a single CPU core
  - 9x overall application speedup vs. 8 CPU cores
  - 32% faster overall than 8 nodes of G80 cluster
  - GT200 CUDA kernel is 54% faster
  - ~8% variation in GPU load
- Cost of double-precision for force accumulation is minimal: only 8% slower than single-precision



GPU Kernel Performance, May 2008

GeForce 8800GTX w/ CUDA 1.1, Driver 169.09

http://www.ks.uiuc.edu/Research/gpu/

Calculation / Algorithm	Algorithm class	Speedup vs. Intel QX6700 CPU core
Fluorescence microphotolysis	Iterative matrix / stencil	12x
Pairlist calculation	Particle pair distance test	10-11x
Pairlist update	Particle pair distance test	5-15x
Molecular dynamics non-bonded force calc.	N-body cutoff force calculations	10x 20x (w/ pairlist)
Cutoff electron density sum	Particle-grid w/ cutoff	15-23x
MSM short-range	Particle-grid w/ cutoff	24x
MSM long-range	Grid-grid w/ cutoff	22x
Direct Coulomb summation	Particle-grid	44x

Lessons Learned

- GPU algorithms need fine-grained parallelism and sufficient work to fully utilize the hardware
- Fine-grained GPU work decompositions compose well with the comparatively coarse-grained decompositions used for multicore or distributed memory programing
- Much of GPU algorithm optimization revolves around efficient use of multiple memory systems and latency hiding

Lessons Learned (2)

- The host CPU can potentially be used to “regularize” the computation for the GPU, yielding better overall performance
- Overlapping CPU work with GPU can hide some communication and unaccelerated computation

Multi-core CPUs, Accelerators and Production Software

- A few of my rants about the current state of parallel programming, accelerators…
- Currently, a programmer writes multiple codes for the same kernel, e.g. pthreads, MPI, CUDA, SSE, straight C, …
- Error, exception handling in a multi-kernel environment can be quite tricky, particularly if buried within child threads, with various other operations in-flight already

Multi-core CPUs, Accelerators and Production Software (2)

- Current APIs are composable, but can get quite messy:
  - Combinatorial expansion of multiple APIs and techniques leads to significant code bloat
  - Pure library-based interfaces are particularly unwieldy due to code required for packing/unpacking function parameters
  - Simple pthreads code can quickly bloat to hundreds of lines of code if there are many thread-specific memory allocations, parameters, etc to deal with
- Current systems do very little with NUMA topology info, CPU affinity, etc

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- Additional Information and References:
  - **http://www.ks.uiuc.edu/Research/gpu/**
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  - NCSA GPU Cluster
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- NIH funding: P41-RR05969

Publications

http://www.ks.uiuc.edu/Research/gpu/

- Adapting a message-driven parallel application to GPU-accelerated clusters. J. Phillips, J. Stone, K. Schulten. *Proceedings of the 2008 ACM/IEEE Conference on Supercomputing*, *(in press)*
- GPU acceleration of cutoff pair potentials for molecular modeling applications. C. Rodrigues, D. Hardy, J. Stone, K. Schulten, W. Hwu. *Proceedings of the 2008 Conference On Computing Frontiers*, pp. 273-282, 2008.
- GPU computing. J. Owens, M. Houston, D. Luebke, S. Green, J. Stone, J. Phillips. *Proceedings of the IEEE*, 96:879-899, 2008.
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- Continuous fluorescence microphotolysis and correlation spectroscopy. A. Arkhipov, J. Hüve, M. Kahms, R. Peters, K. Schulten. *Biophysical Journal*, 93:4006-4017, 2007.