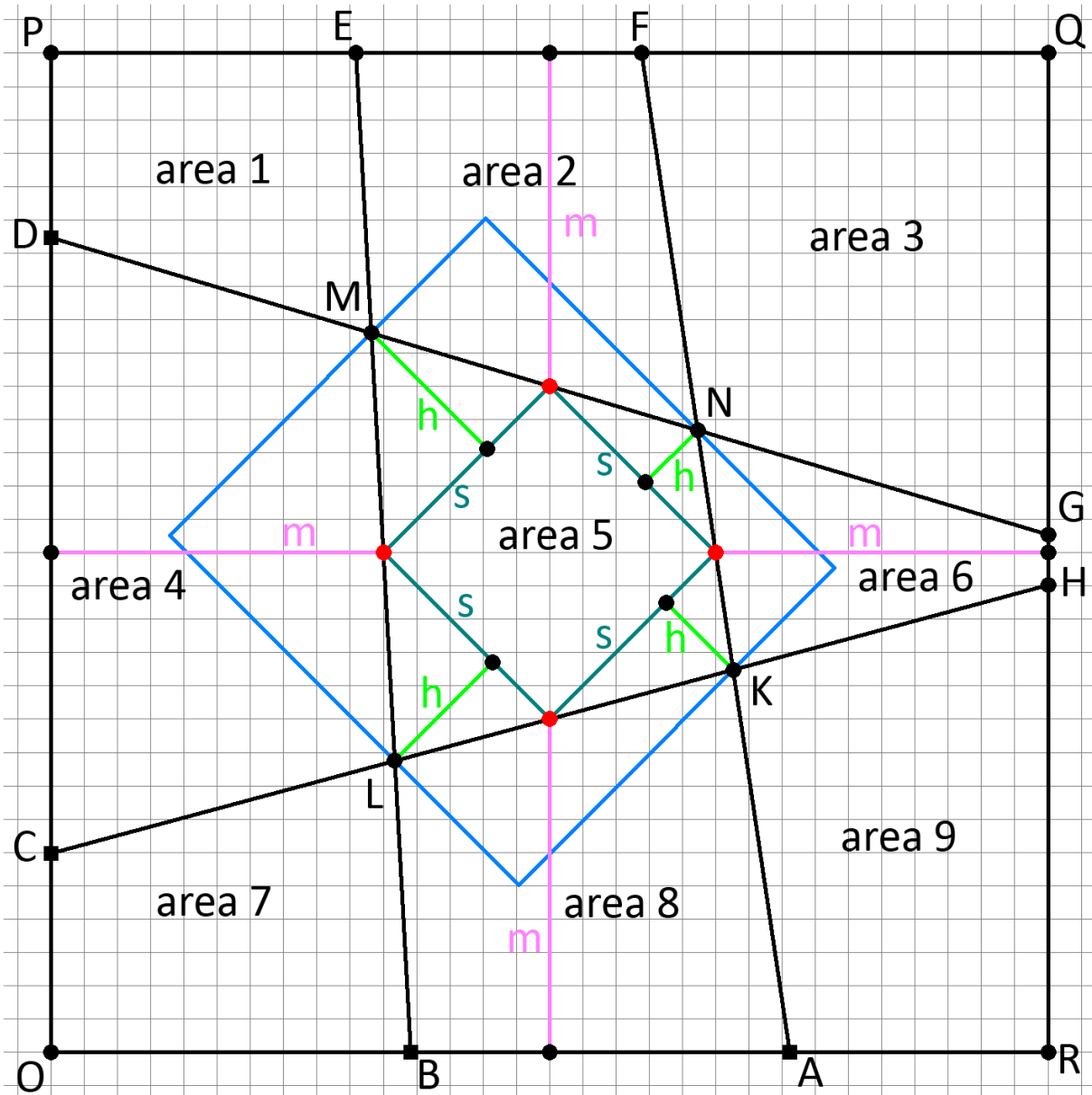


# Theory of area magic squares



Say  $S$  is the magic sum, then  $\text{area}1 + \text{area}2 + \text{area}3 = S$ . The sum of all 9 areas has to be  $3 \cdot S$ .

This means the trapezoid  $DGQP = \text{area}1 + \text{area}2 + \text{area}3 = S = 1/3$  of the whole area.

$\Rightarrow$  The middle parallel  $m$  has to be  $1/3$  of the length of the square.

$\Rightarrow$  The 4 straight lines have to run through the red points.  $\Leftrightarrow$  areas make semi-magic square

In a magic square of order 3 the number of the center cell has to be  $1/9$  of the sum of all numbers.

$\Rightarrow \text{area}5 = KLMN = m \cdot m = 2s^2$  (1)

$KLMN = s^2 + 4 \text{ triangles} = s^2 + \frac{1}{2} s \cdot \Sigma h = \frac{1}{2} s(2s + \Sigma h)$  (2)

(1) and (2)  $\Rightarrow 2s = \frac{1}{2}(2s + \Sigma h) \Leftrightarrow 4s = 2s + \Sigma h = \frac{1}{2}$  (circumference of blue rectangle) (*difficult!*)

I did not use the second criterion for the calculation. You may forget the blue rectangle. It is just a nice geometric gimmick. It is enough to know this:  $\text{area}5 = 1/9$  of the whole area